

(ii) Maximum power density,

$$\begin{aligned}\frac{P_{\max}}{A} &= \frac{8}{27} \rho V_i^3 \\ &= \frac{8}{27} \times 1.226 \times (15)^3 = 1226 \text{ W/m}^2.\end{aligned}$$

(iii) Assuming efficiency,  $\eta = 35\%$

Actual power density,

$$\frac{P}{A} = 0.35 \times 2068.87 = 724 \text{ W/m}^2$$

(iv) Total power produced,

$$P = \text{Power density} \times \text{Area}$$

$$\begin{aligned}&= 724 \times \frac{\pi}{4} (120)^2 \\ &= 8184 \times 10^3 \text{ W} = 8184 \text{ kW}\end{aligned}$$

(v) Torque at maximum efficiency

$$\begin{aligned}T &= \frac{2}{27} \frac{\rho D V_i^3}{N} \\ &= \frac{2}{27} \times \frac{1.226 \times 120 \times (15)^3}{(40/60)} = 55170 \text{ N}\end{aligned}$$

(vi) Maximum axial thrust

$$\begin{aligned}F_{x_{\max}} &= \frac{\pi}{9} \rho D^2 V_i^2 \\ &= \frac{\pi}{9} \times 1.226 \times (120)^2 \times (15)^2 \\ &= 1385870 \text{ N}\end{aligned}$$

#### 4.7. WIND TURBINE OPERATION AND CONTROL

The power output of a wind mill is proportional to square of its diameter<sup>3</sup> cube of the wind velocity.

