

### Assignment 3 (Unit 3)

1. Find the stiffness and flexibility influence coefficients of the system shown in figure below

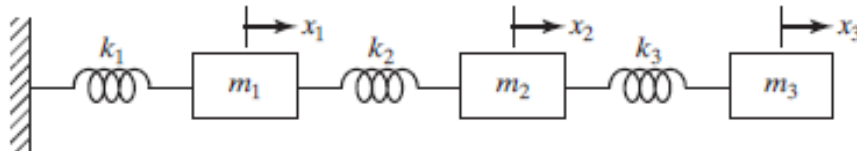


Figure 1

2. Derive the flexibility matrix of the weightless beam shown in Figure below. The beam is simply supported at both ends, and the three masses are placed at equal intervals. Assume the beam to be uniform with stiffness  $EI$ .

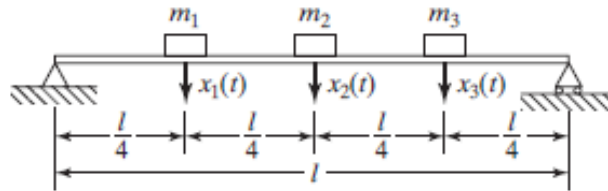


Figure 2

3. State the free-vibration equations of motion of the system and also find the natural frequencies and mode shapes of the system shown below for  $k_1 = k_2 = k_3 = k$  and  $m_1 = m_2 = m_3 = m$

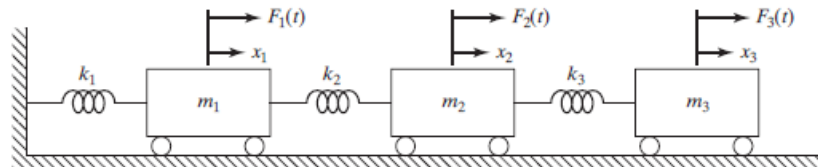


Figure 3

4. Show how flexibility influence coefficients are used to obtain fundamental natural frequency of a system shown in figure 4 below by Stodola method.

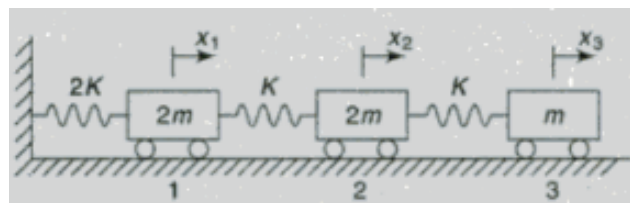


Figure 4

5. Find the lowest natural frequency and modal vector of the system shown in figure 4 by matrix iteration method. Draw mode shape.

6. Find the natural frequencies of an unrestrained system shown in figure 5.

$$J_1 = J_2 = J_3 = J; K_{11} = K_{12} = K_{13}$$

Use Lagrange's equation to get differential equations of motion.

$$T = \frac{1}{2} (J\dot{\theta}_1^2 + J\dot{\theta}_2^2 + J\dot{\theta}_3^2)$$

$$V = \frac{1}{2}k[(\theta_2 - \theta_1)^2 + (\theta_3 - \theta_2)^2]$$

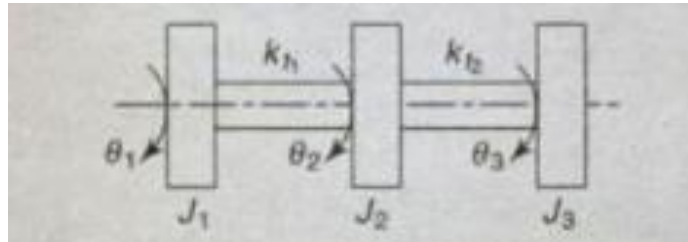


Figure 5

7. Rotor of a turbocharger of 9 kg mass is keyed centrally to a shaft of 25 mm diameter, 40 cm length between bearings. Shaft material density = 8 gm/cm<sup>3</sup>; and shaft may be treated as simply supported. Find (i). critical speed (ii) Amplitude of rotation of rotor at 3200 rpm if eccentricity of rotor CG = 0.015 mm (iii) vibratory force transmitted to base

#### Reference books:

1. Dynamics of Machinery by FarazdakHaideri, 5<sup>th</sup> Edition, NiraliPrakashan
2. Mechanical Vibrations by S.S.Rao, Fifth Edition, Pearson Publicaton