## Plane wave method for DFT calculations

## Wavefunction $(\Psi)$

- Numerical representation of orbitals / wave functions is necessary for computation.
- It has to be
- Compact
- Efficient
- Accurate
- It should be accurate $\left(-\nabla^{2}\right)$ derivatives to calculate K.E.



## Recap

- The effective Hamiltonian,

$$
\left[\widehat{T}_{i}+\widehat{V}_{\text {ion }}+\widehat{V}_{H}+\widehat{V}_{X C}\right] n(r)=E n(r)
$$

- The density of electrons is represented in terms of wavefunction such as,

$$
n(r)=\sum_{i}^{o c c}\left|\psi_{i}(r)\right|^{2}
$$

- We know that the wavefunctions $\psi$ is expressed in a basis set or basis function,

$$
\psi=\sum c_{i} \phi_{i}
$$

- The basis set is expressed'in terms of Gaussian function. Hence it is called as Gaussian Basis sets. There are different types of Gaussian functions.
- Gaussian basis sets expression is like

$$
\psi_{i}=\sum_{j} c_{j} e^{-\alpha_{r} Y_{K}(\tilde{r})}
$$

## Gaussian Basis Set

- Parallel efficient
- Uses different basis sets for molecules and solids
- Expensive to calculate pulay terms such as forces, stresses and force constants
- It consider all electron for
 calculations


## Plane wave basis sets

- Wave vectors (G) are defined in reciprocal lattice vectors which help for periodicity constraint.

$$
\vec{G}_{i i i,}=\left(i_{1}-\frac{N_{1}}{2}\right) \vec{b}_{1}+\left(i_{2}-\frac{N_{2}}{2}\right) \vec{b}_{2}+\left(i_{3}-\frac{N_{3}}{2}\right) \vec{b}_{3}
$$

Where $b_{1}, b_{2}$ and $b_{3}$ are reciprocal lattice vectors.

- The plane wave basis sets is,

$$
\psi_{i, k}(r)=\sum_{G}^{|G| G_{G}} c_{i, k} G e^{i(k+G) \cdot r}
$$

- Fast Fourier

Transformation (FFT) algorithms used for real and reciprocal space transformations.

- Allow to use more number of atoms.
- Possible to use all electron or only valence electron for calculations.
- Same basis set for
 molecules and solids.
- Eigen values gives band structure.
- Electrons fill lowest energy state.
- Energy between highest occupied state and lowest unoccupied state gives the Fermi energy




## Band structure related properties

- Optical properties
- Excitation energies
- Electronic transport
- Electron-phonon interactions
- Etc.


## Optical Property of $\mathrm{Srl}_{2}$

Near optical isotropy in noncubic $\mathrm{Srl}_{2}$ : Density functional calculations D. J. Singh ${ }^{\text {a) }}$

Materials Science and Technology Division and Center for Radiation Detection Materials and Systems, Oak Ridge National Laboratory, Oak Ridge. Tenuessee 37831-6114, USA
(Received 24 March 2008; accepted 1 May 2008; published online 22 May 2008)


FIG. 4. (Color online) Wavelength dependent refractive index of $\mathrm{SrI}_{2}$ as obtained with the Engel-Vosko GGA.

Fabrication and Properties of $\mathrm{Translucent} \mathrm{SrI}_{2}$ and $\mathrm{Eu}: \mathrm{SrI}_{2}$ Scintillator Ceramics
Stephen R. Podowitz, Romain M. Gaumé, Wesley T. Hong. Atlal Laouar, and Robert S. Feigelson


Fig. 5. Translucent ceramic sample of 0.77 mm-thick $\mathrm{Eu}: \mathrm{SrI}_{2}$ backlit.

## Magnetic property of $\mathrm{Fe}_{2} \mathrm{Ti}$

| Phase | End members | Pearson <br> sympol | $\Delta E_{f}$ | Magnetism |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Fe}_{2} \mathrm{Ti}$ | $(\mathrm{Fe})_{2}(\mathrm{Ti})_{4}(\mathrm{Fe})_{6}$ | $h P 16$ | -30.131 | FM |
|  |  | $h P 16$ | -29.817 | AFM <br> $\left(\mu_{B}=1.417\right)$ |
|  |  | $h P 16$ | -27.134 | PM |




FM


Figure 4.3: Unit cell of $\mathrm{Fe}_{2} \mathrm{Ti}$ in C14 Laves crystal structure. PM, FM and AFM indicates para, ferro and antiferro magnetiam of Laves phase reapectively. Fe atoms cocupies ( 2 a ) and ( 6 h ) sites and Ti atome occupies (4f) sites.

