

# AC MOTORS

*Subject Name: Electrical Fundamentals*

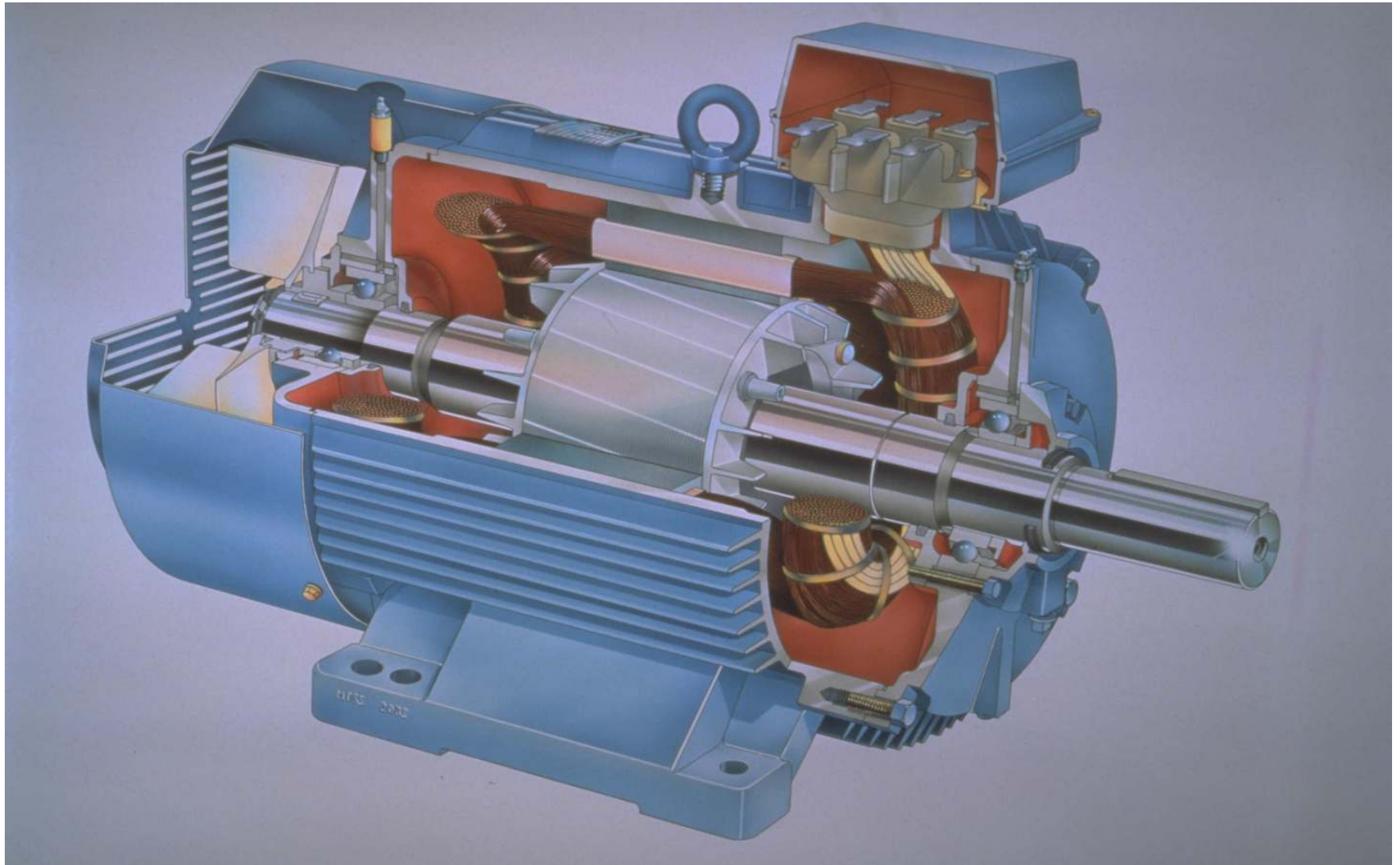
Prepared By:  
Nikesh I Patel

Approved By:

# INDEX

<b>Sr. No.</b>	<b>Topic</b>
1	Construction ,principle of operation and characteristics of AC synchronous and Induction motors both single & three phase .
2	Squirrel cage and slip ring rotor construction
3	Production of rotating magnetic field theory
4	Slip , speed and rotor frequency concept
5	Power stage diagram of an IM
6	Torque Equation
7	Torque-slip and torque-speed characteristics
8	Losses in induction motor
9	Working principle & construction of single phase induction motor
10	Double field revolving theory
11	Types of single phase induction motor

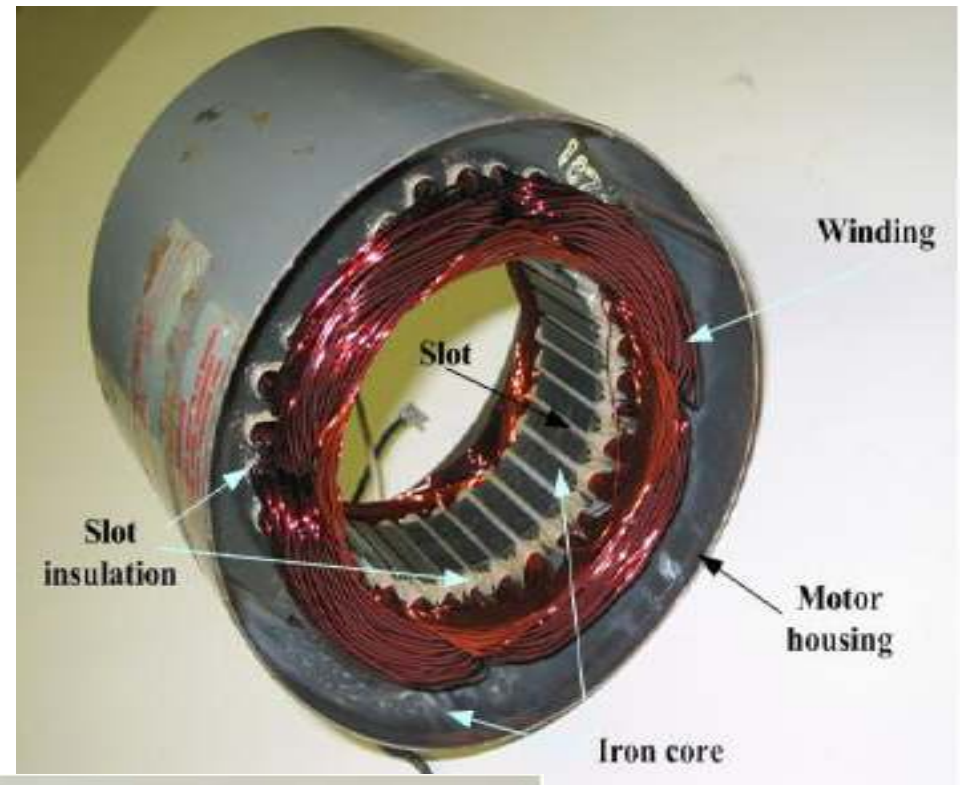
# 3-phase Induction Motor



# Construction

➤ An induction motor has two main parts

1. Stator
2. Rotor



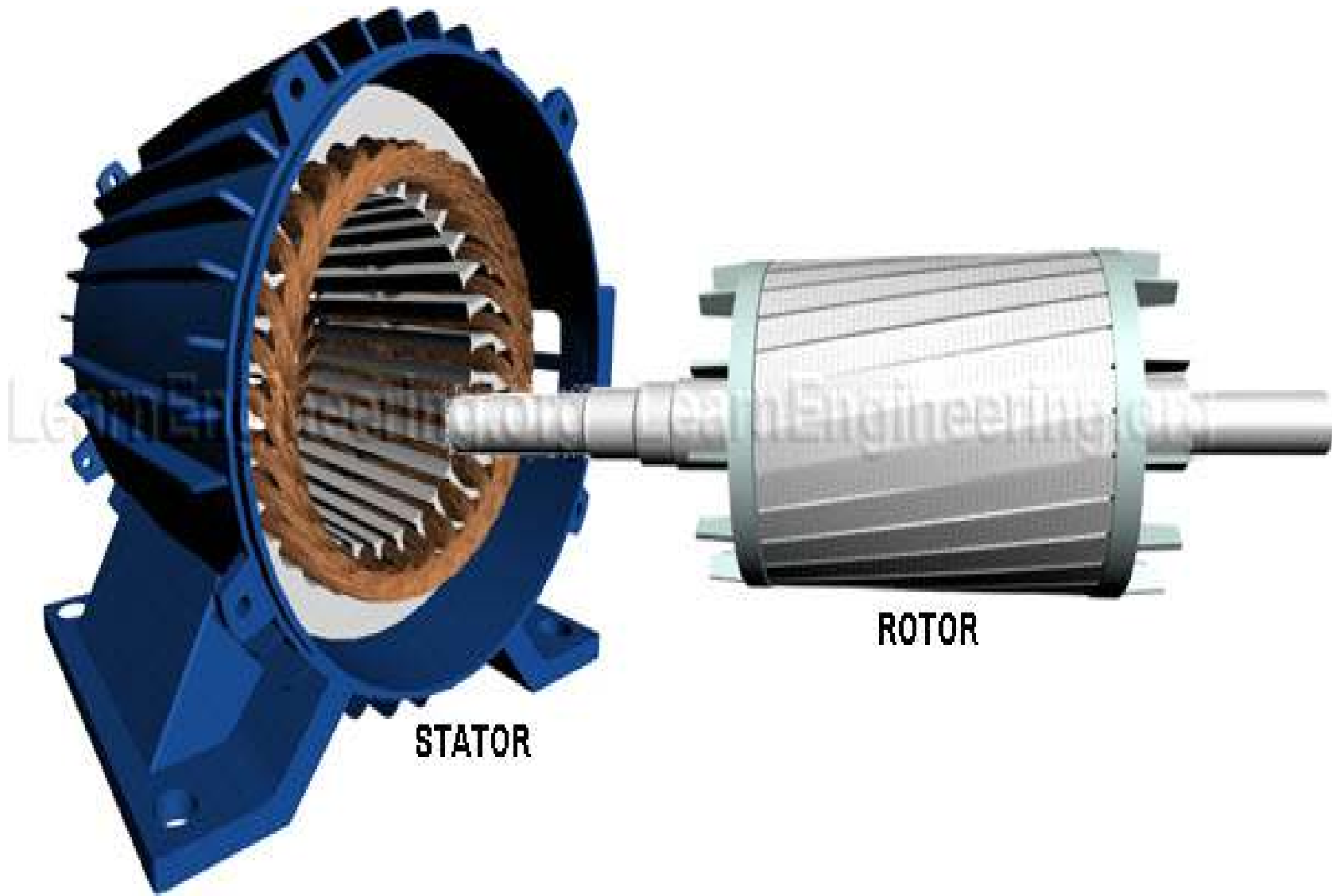
# Construction

➤ A three phase Induction motor essentially consists of two parts:

1. STATOR
2. ROTOR

## STATOR

- A Stator is a stationary part and Rotor is the rotating part.
- The Stator is built up of high-grade alloy steel lamination to reduce eddy-current losses.
- The laminations are slotted on the inner periphery and are insulated from each other.
- The insulated stator conductors are placed in these slots.
- The Stator conductor are connected to form a three-phase winding.
- The three phase winding may be Star or Delta connection.

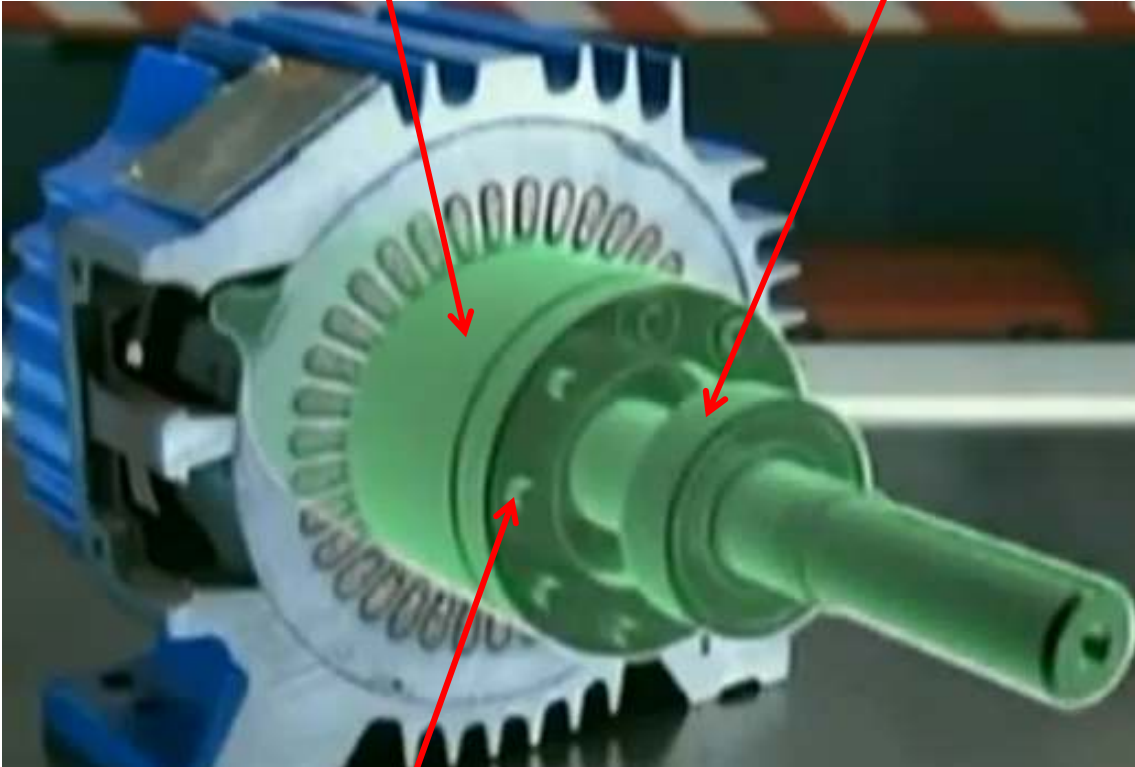
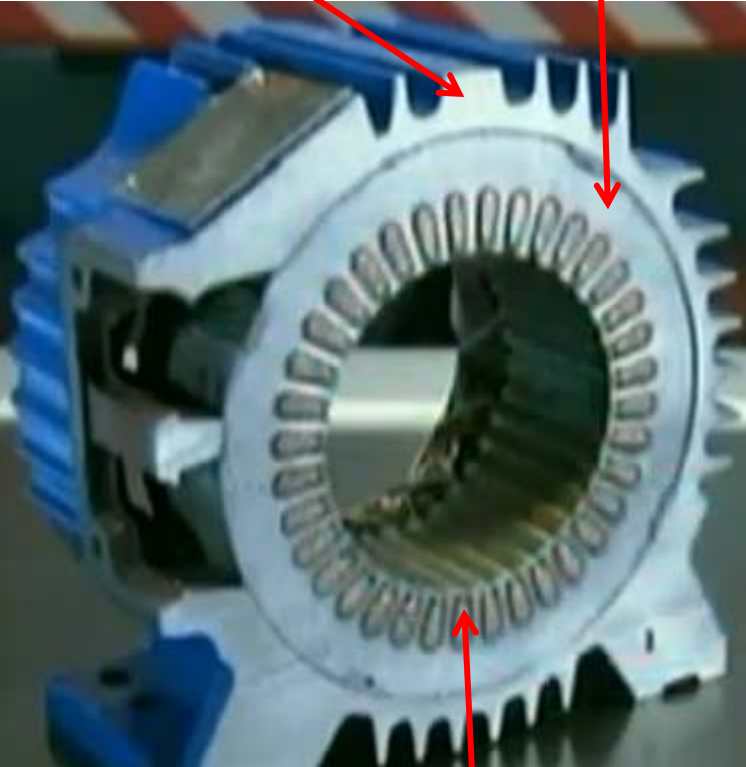


**Frame**

**Stator Core**

**Rotor**

**Bearings**



**Stator winding**

**Rotor winding**

# *Stator*

<b>Parts</b>	<b>Material used</b>	<b>Work</b>	<b>Remarks</b>
Stator Frame	Cast Iron	Provide Support	No Flux Passes
2 End covers	Cast Iron	Provide Support	
Stator Core	Laminated Silicon Steel	Hold windings	Provide flux Path
Distributed winding	Copper	Generate flux	High Conductivity
Bearings		Smooth rotation of shaft	





FRAME



STEEL LAMINATIONS

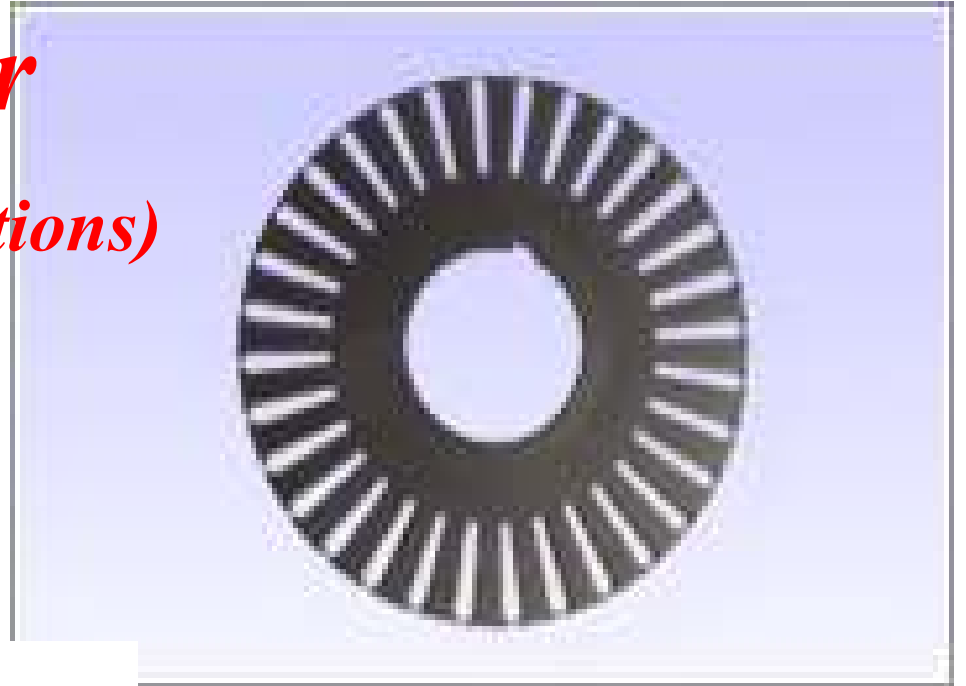




# ROTOR

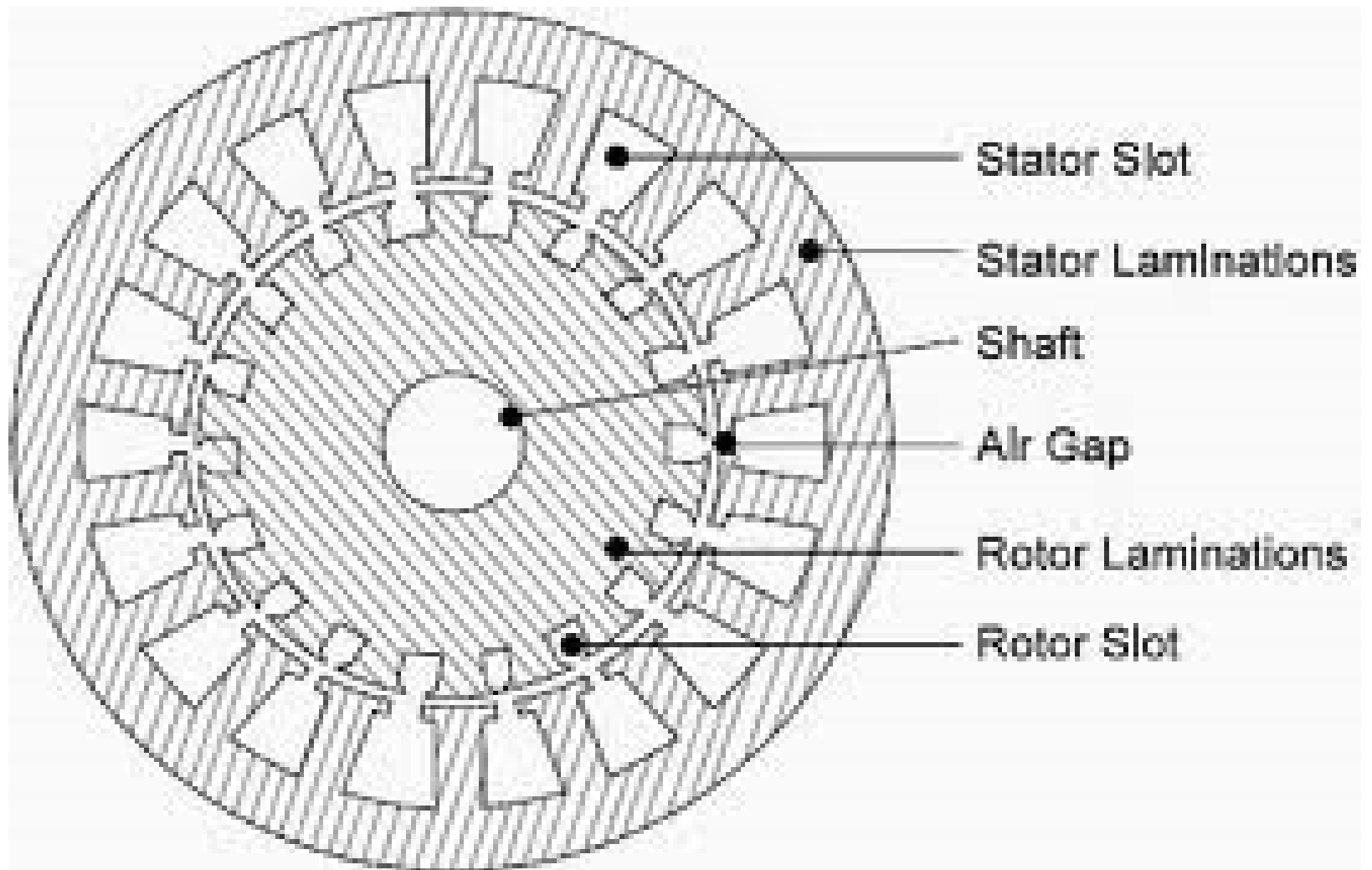
- The Rotor is built up of thin laminations of the high-grade alloy steel material.
- The laminated cylindrical core is mounted directly on the shaft or a spider carried by the shaft.
- There are two type of Induction Motor Rotor :
  1. Squirrel-cage rotor or simply cage rotor.
  2. Phase wound or wound rotor. Motor using this type of rotor are also called slip-ring motor.

***Rotor***  
***(Laminations)***





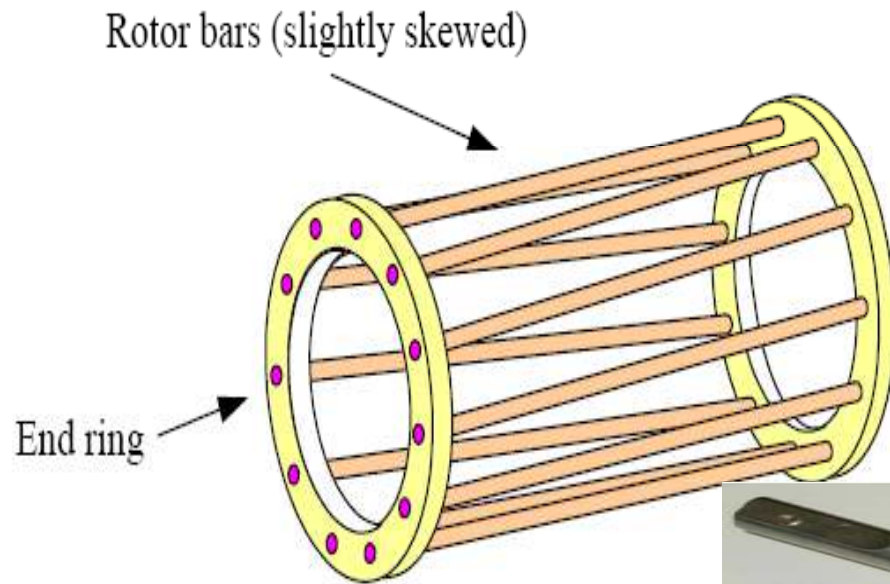
IRON LAMINA



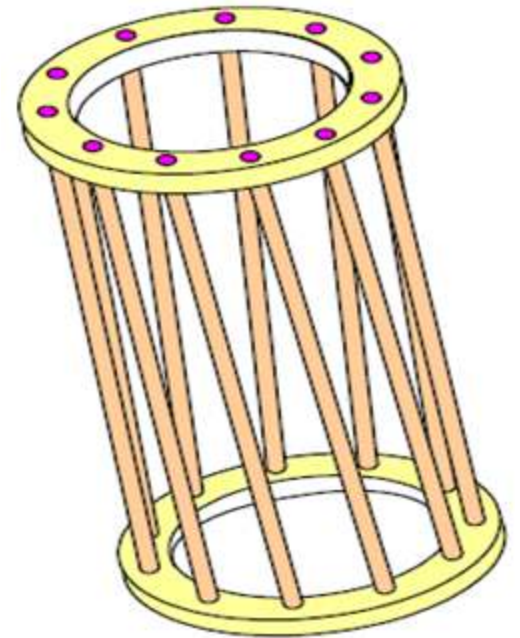
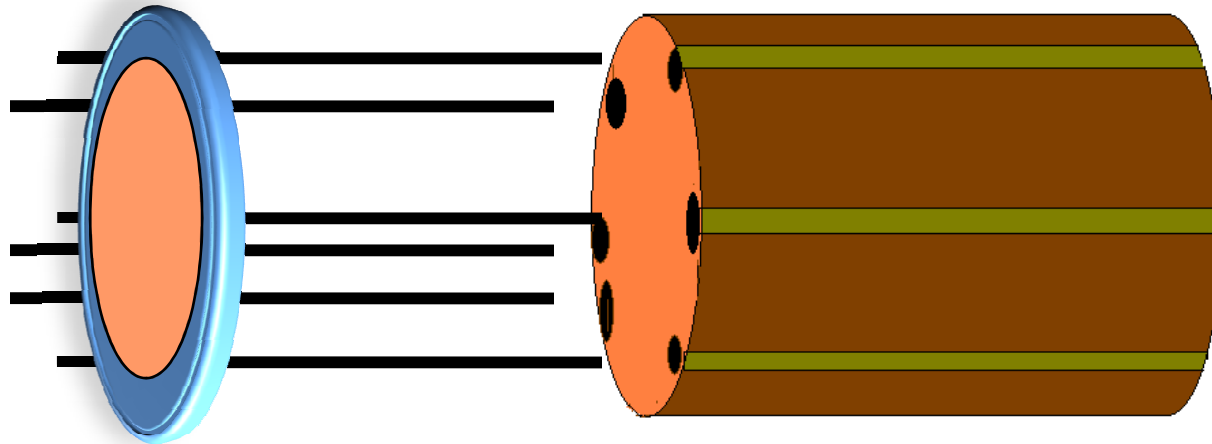
# Rotor

Types:

1. Squirrel-cage rotor
2. wound-rotor



# *Squirrel-cage rotor*

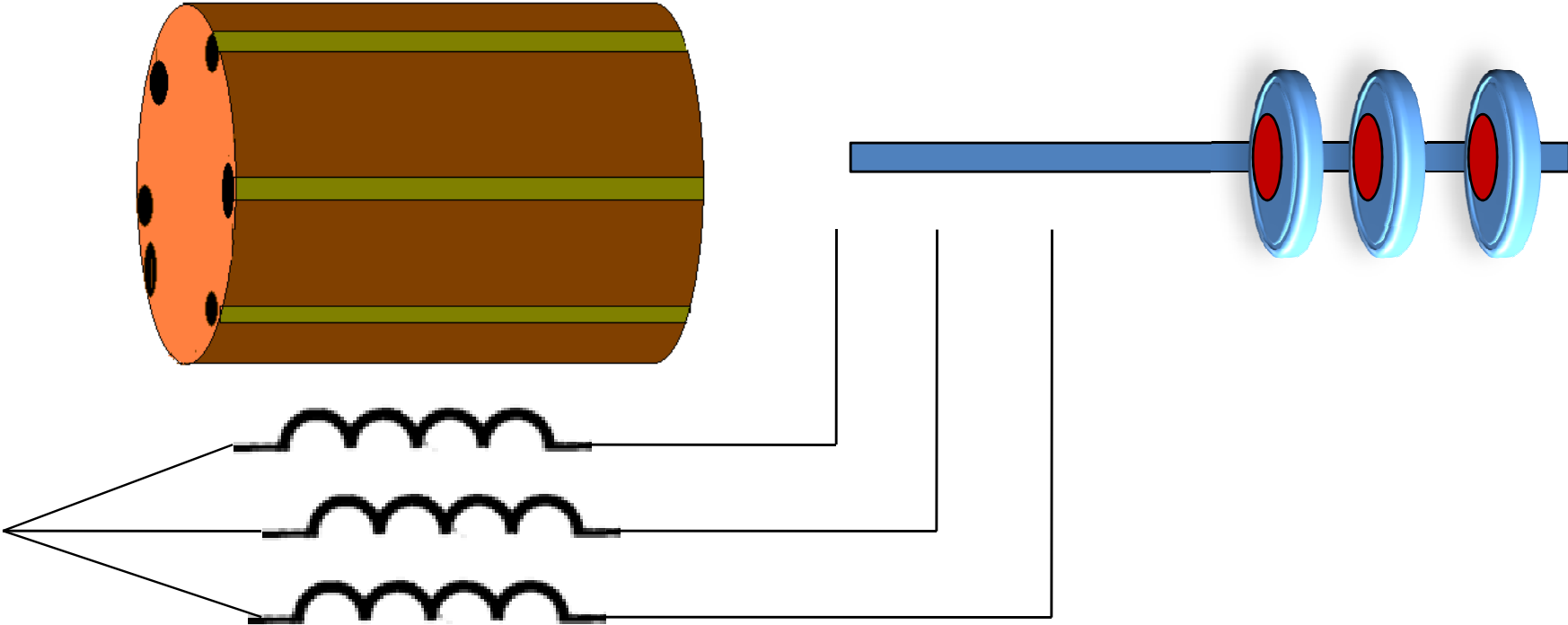
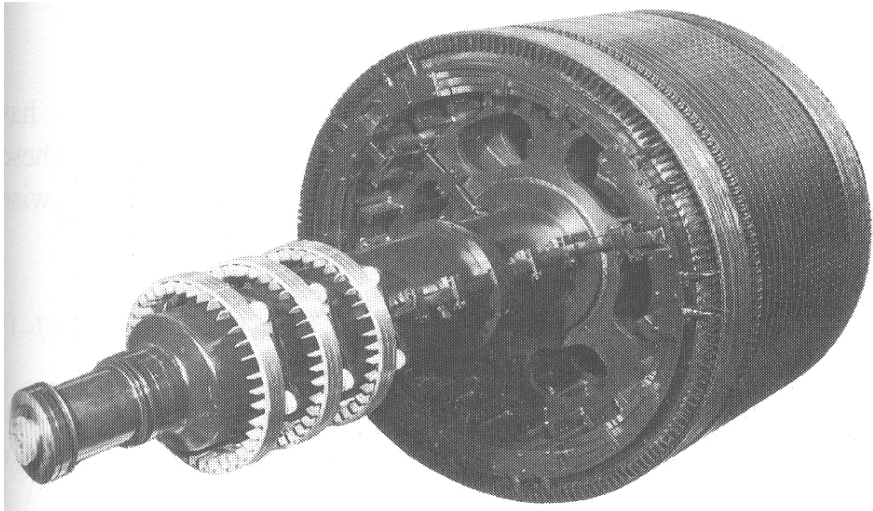


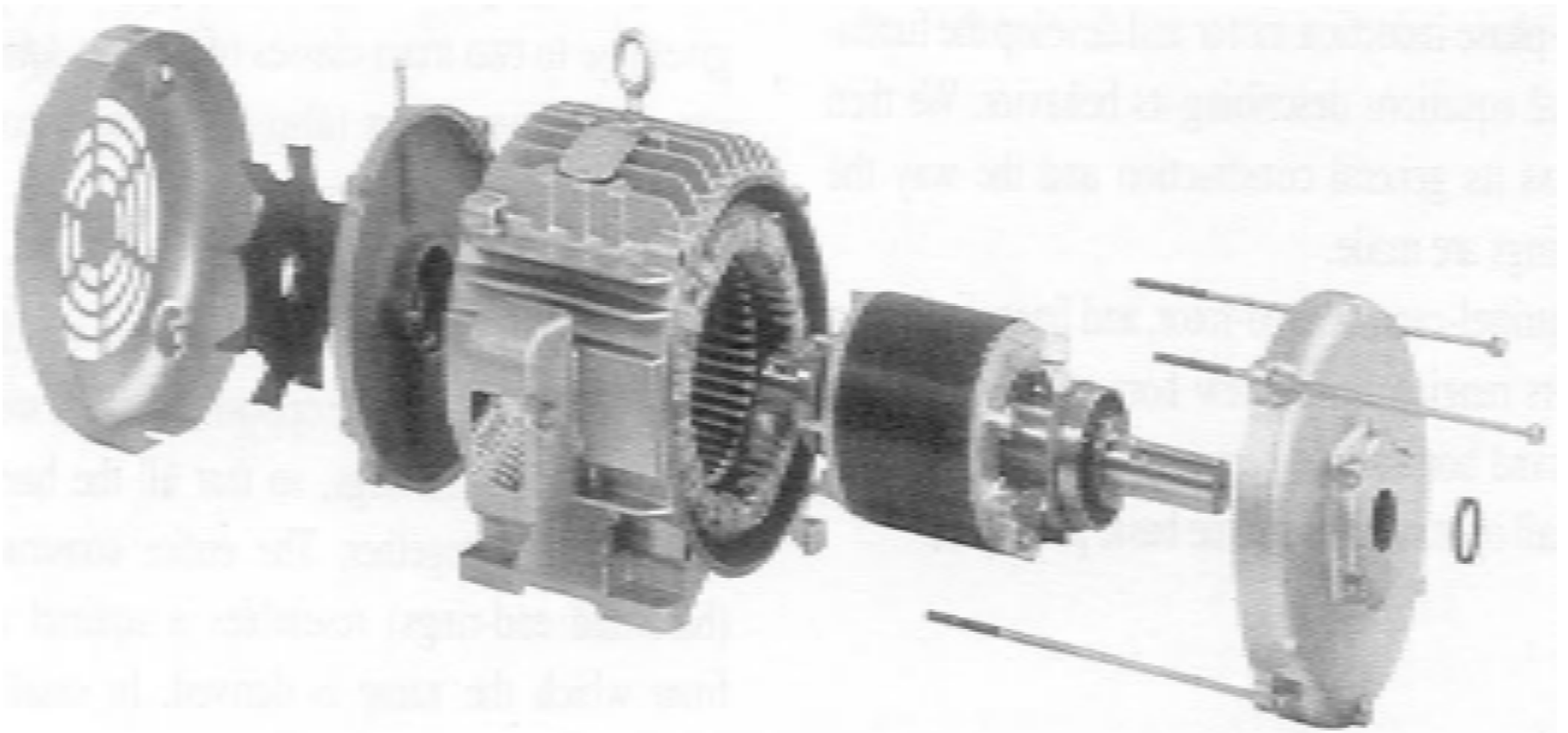


## ➤ Advantages of Squirrel Cage IM

1. Absence of brushes reduce the risk of sparking
2. Smooth Operation
3. More uniform torque is produced and the noise is reduced during operation
4. Less maintained
5. Higher efficiency and higher power factor
6. Locking tendency of the rotor is reduced. During locking the rotor and stator teeth attract each other due to magnetic action

*Wound-rotor(Slip Ring)*

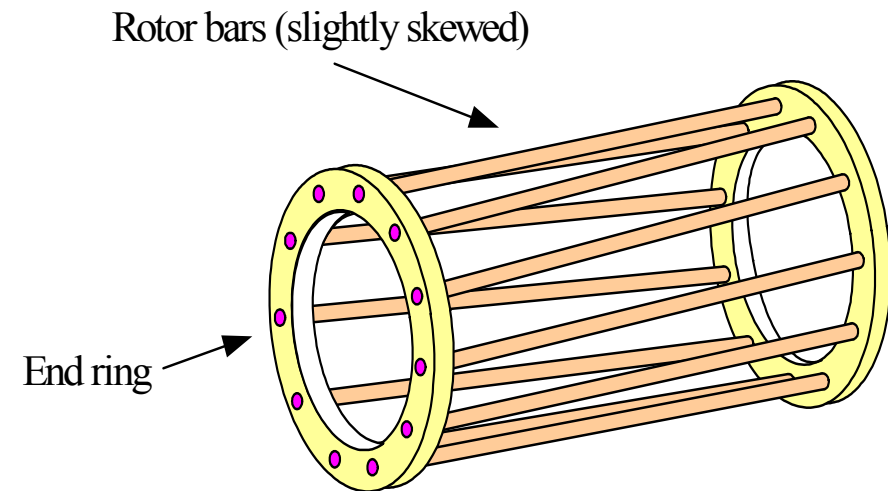




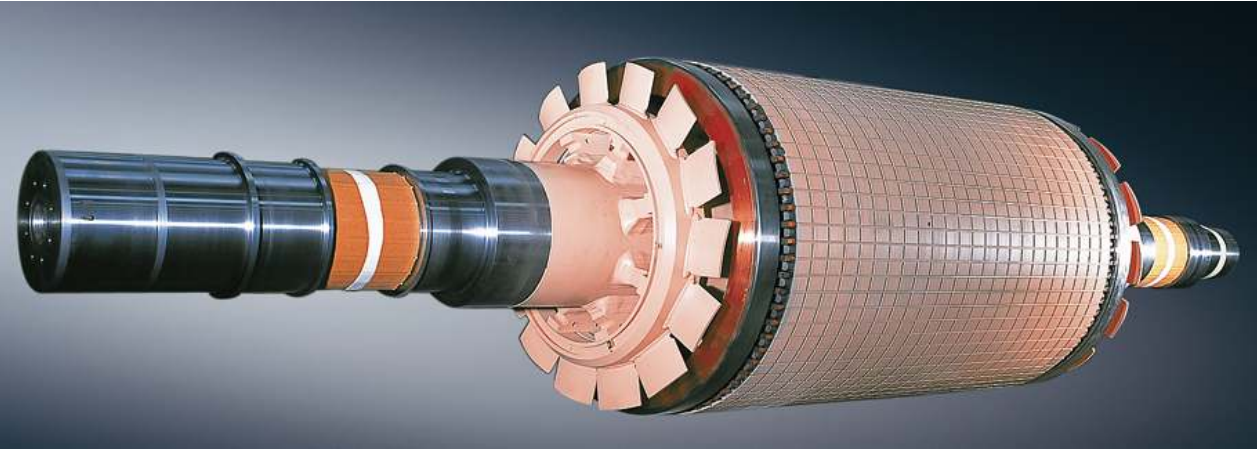
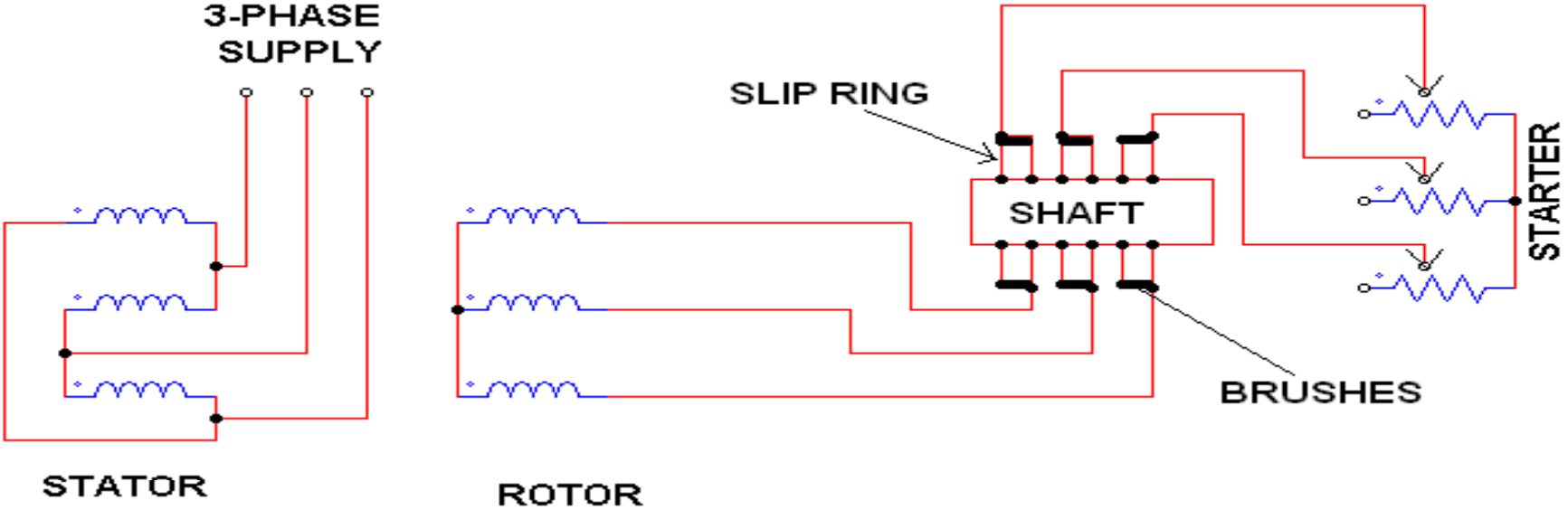
- In induction Machine Rotor windings (Bars) have current by only induction

# 1. Squirrel-Cage Rotor

➤ The conductors and the end rings form a cage of the type which was once commonly used for keeping squirrels.



# 2. Wound Rotor or Slip Ring Rotor



➤ Rotor winding is exactly similar to Stator

➤ To increase the starting torque and decrease the starting current

from the supply

➤ To control the speed of motor

## ❖ Comparison of Squirrel cage and Wound Rotor

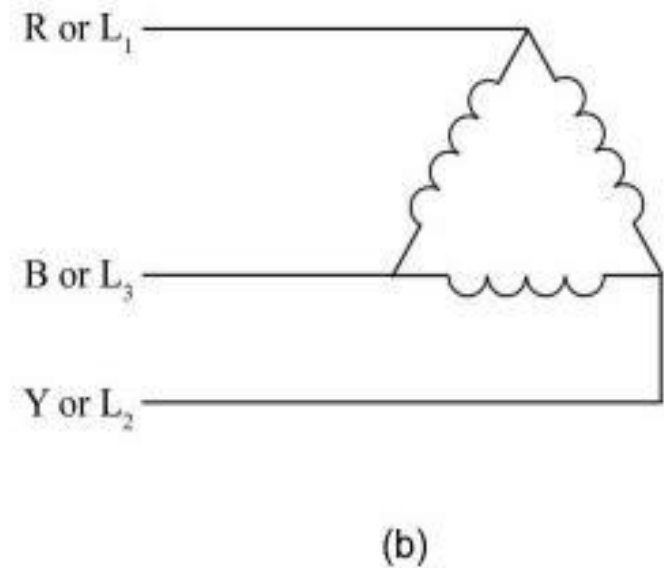
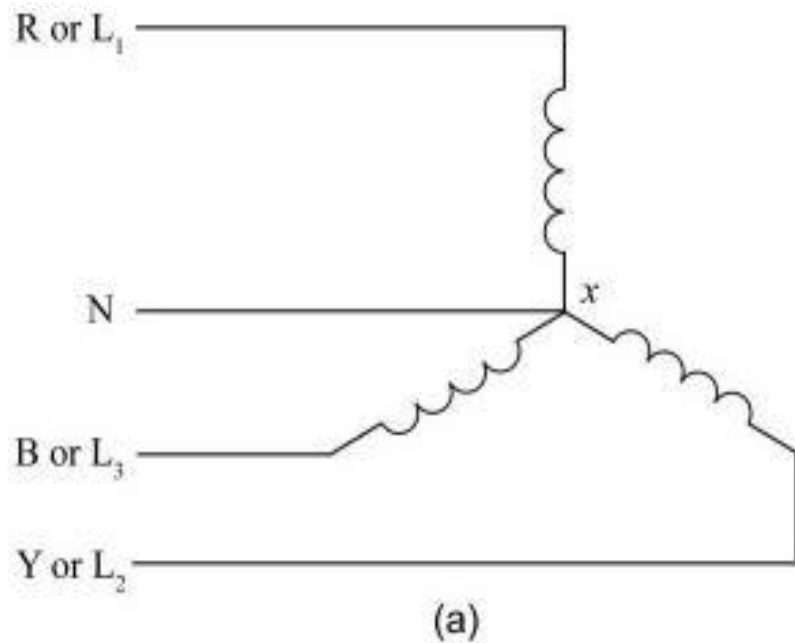
<b>Slip ring Rotor</b>	<b>Squirrel Cage Rotor</b>
Rotor consists of 3-phase winding similar to stator winding	Rotor consist of bars which are shorted at the ends with the help of end rings
Construction is complicated	Construction is simple
External resistance is added	As permanently shorted, External resistance can't be added
Slip ring and brushes are presents	Slip ring and brushes are not presents
Rotor are costly	Rotor are cheap
Maintenance are required	Maintenance free
Higher starting Torque	Moderate Starting Torque
Speed control is possible	Speed control Not possible
Rotor Cu-loss is high so efficiency is low	Rotor Cu-loss are less, so efficiency is high
Use for lifts, hoists, cranes, elevators, compressor etc..	Use in lathes, drilling machine, fan, blower, water pumps, grinder, etc..

## ROTATING MAGNETIC FIELD(R.M.F)

- 3-Phase IM is based on the principle of rotating magnetic fields.

### PRODUCTION OF R.M.F.

- Stationary part: Stator
- 3-phase winding is connected in star or delta
- Each winding are displaced from each other by 120 degree.





- 3-phase current are displaced from each other by  $120^{\circ}$  electrical degree.
- Each alternating phase current produces its own flux which is sinusoidal.

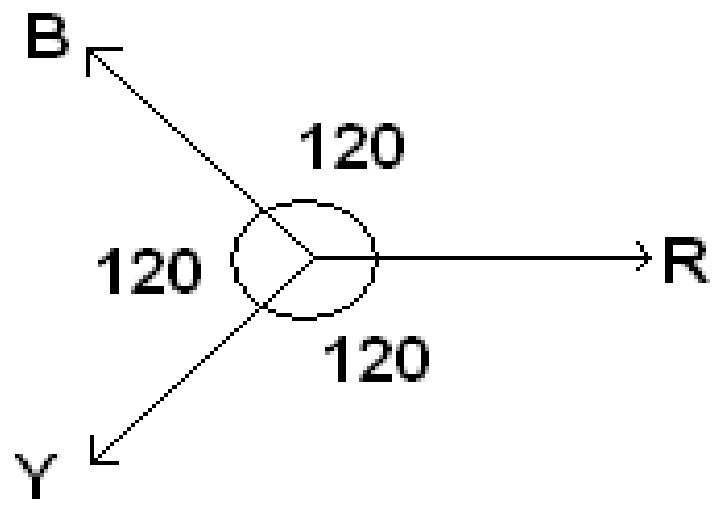
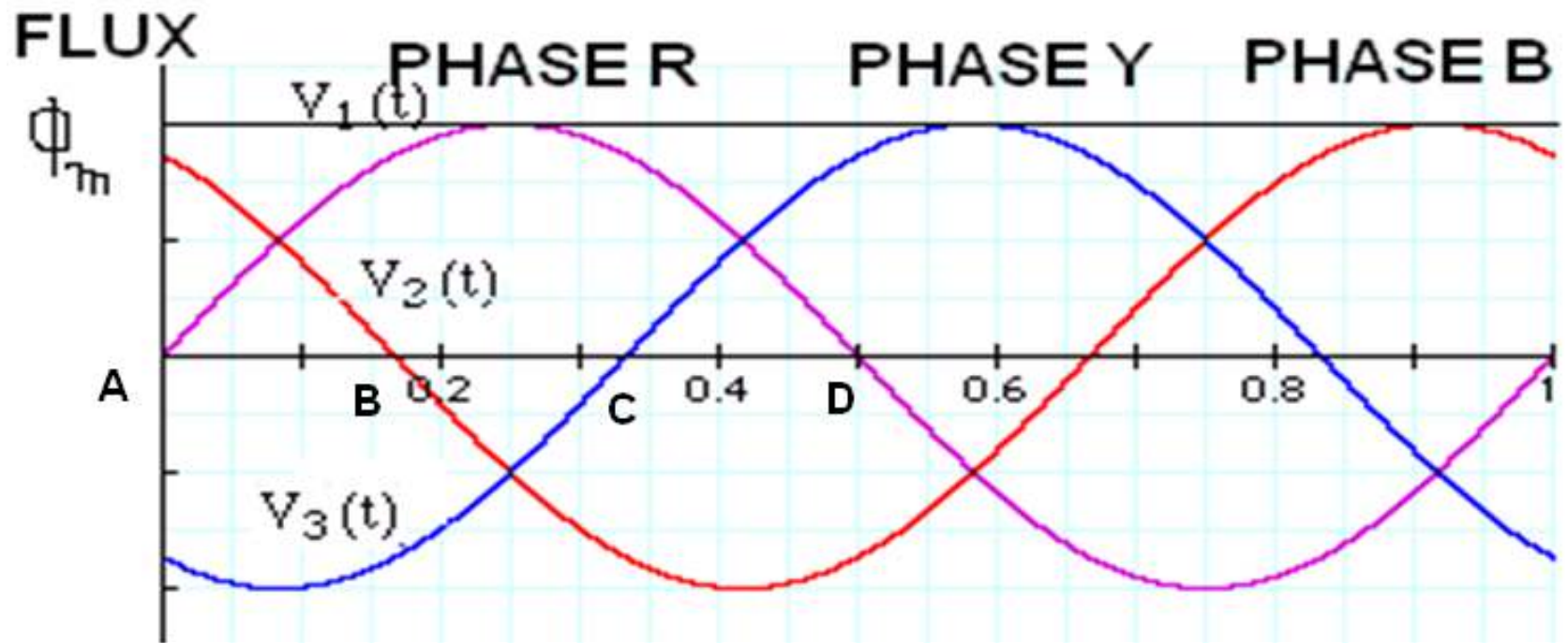
$$\phi_R = \phi_m \sin(\omega t) = \phi_m \sin \theta$$

$$\phi_Y = \phi_m \sin(\omega t - 120^{\circ}) = \phi_m \sin(\theta - 120^{\circ})$$

$$\phi_B = \phi_m \sin(\omega t - 240^{\circ}) = \phi_m \sin(\theta - 240^{\circ})$$

- Resultant flux  $\phi_T$

$$\overline{\phi_T} = \overline{\phi_R} + \overline{\phi_Y} + \overline{\phi_B}$$



A.  $\theta = 0$

B.  $\theta = 60$

C.  $\theta = 120$

D.  $\theta = 180$

CASE-A:  $\theta = 0$

$$\varphi_R = \varphi_m \sin 0 = 0$$

$$\varphi_Y = \varphi_m \sin(0 - 120^\circ) = -0.866 \varphi_m$$

$$\varphi_B = \varphi_m \sin(0 - 240^\circ) = 0.866 \varphi_m$$

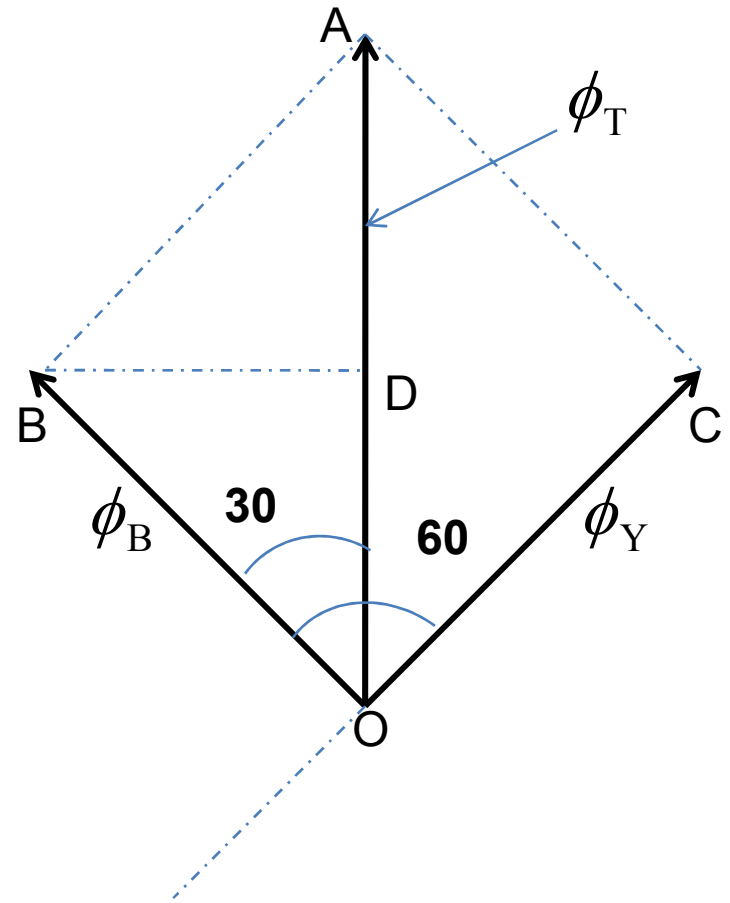
$$OD = DA = \frac{\phi_T}{2}$$

$$\angle BOD = 30$$

$$\cos 30 = \frac{OD}{OB} = \frac{\phi_T \div 2}{0.866 \phi_m}$$

$$\phi_T = 2 \times 0.866 \phi_m \times \cos 30$$

$$\phi_T = 1.5 \phi_m$$



- A.  $\theta = 0$
- B.  $\theta = 60$
- C.  $\theta = 120$
- D.  $\theta = 180$

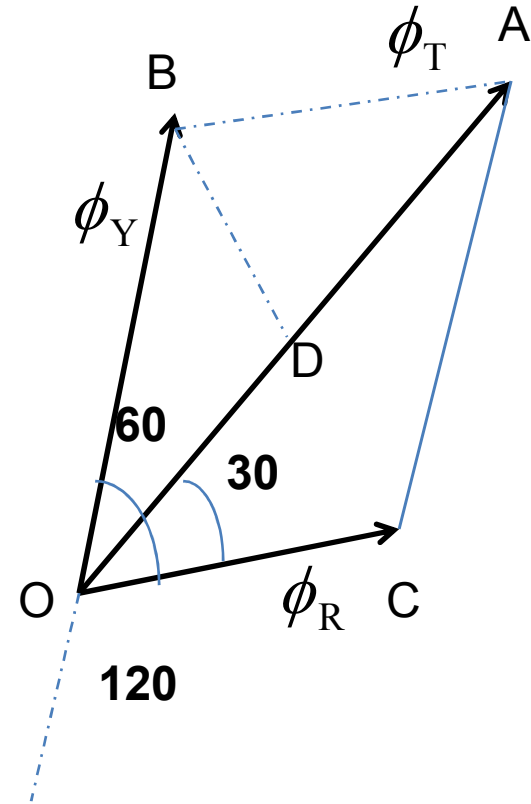
**CASE-B:**  $\theta = 60$

$$\phi_R = \phi_m \sin 60 = 0.866 \phi_m$$

$$\begin{aligned} \phi_Y &= \phi_m \sin(60 - 120) \\ &= -0.866 \phi_m \end{aligned}$$

$$\phi_B = \phi_m \sin(60 - 240) = 0$$

$$\phi_T = 1.5 \phi_m$$



- A.  $\theta = 0$
- B.  $\theta = 60$
- C.  $\theta = 120$
- D.  $\theta = 180$

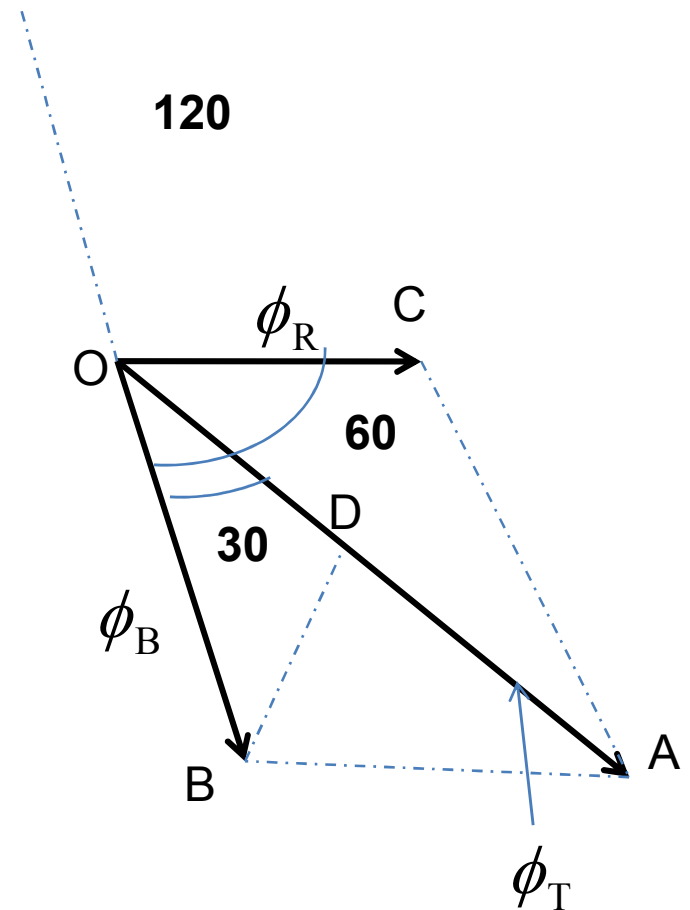
**CASE-C:**  $\theta = 120$

$$\begin{aligned}\varphi_R &= \varphi_m \sin 120^\circ \\ &= 0.866 \varphi_m\end{aligned}$$

$$\begin{aligned}\varphi_Y &= \varphi_m \sin(120^\circ - 120^\circ) \\ &= 0\end{aligned}$$

$$\begin{aligned}\varphi_B &= \varphi_m \sin(120^\circ - 240^\circ) \\ &= -0.866 \varphi_m\end{aligned}$$

$$\varphi_T = 1.5 \varphi_m$$



- A.  $\theta = 0$
- B.  $\theta = 60$
- C.  $\theta = 120$
- D.  $\theta = 180$

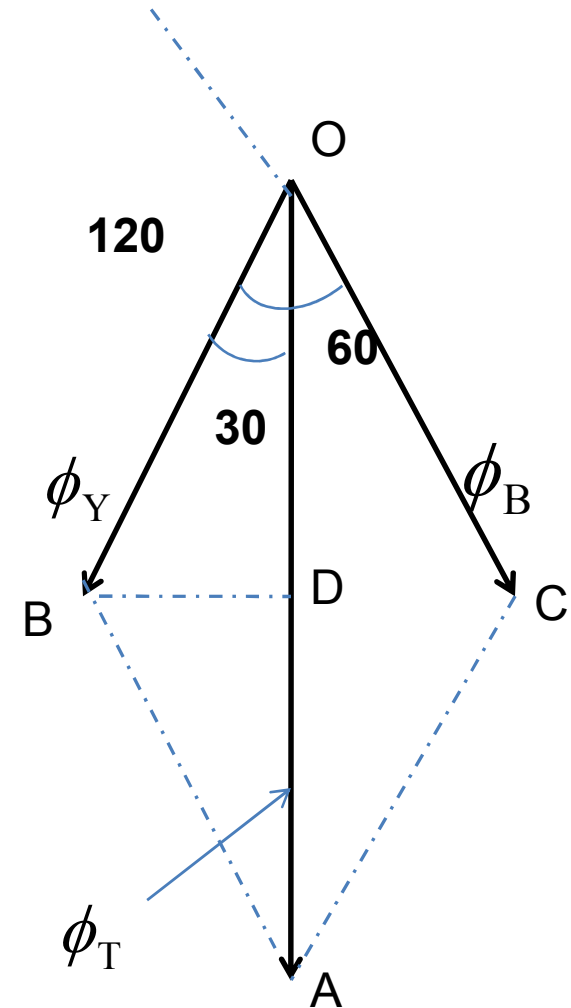
**CASE-D:**  $\theta = 180$

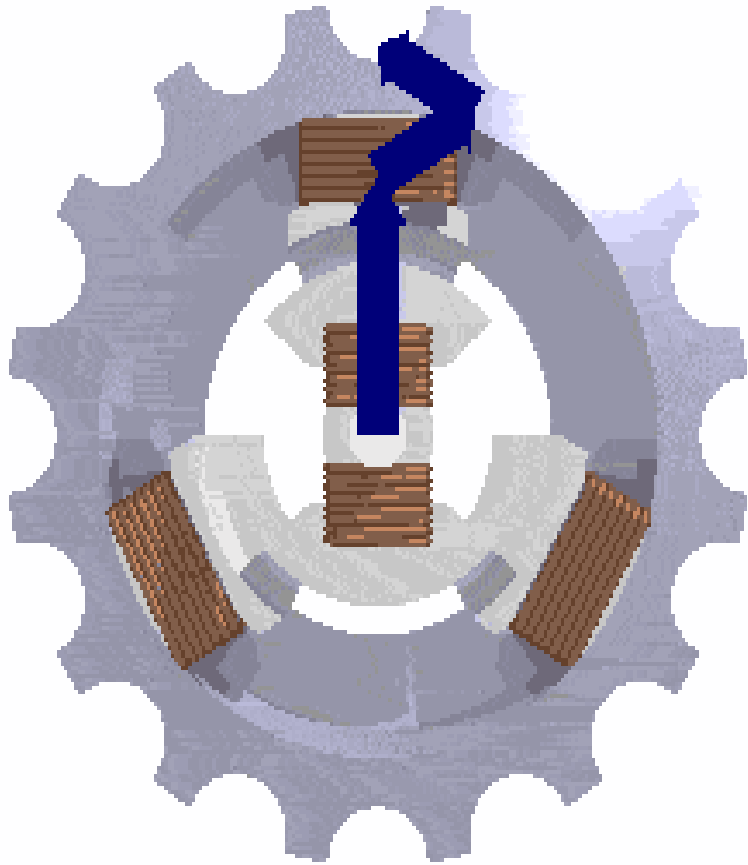
$$\varphi_R = \varphi_m \sin 180 = 0$$

$$\begin{aligned} \varphi_Y &= \varphi_m \sin(180 - 120) \\ &= 0.866 \varphi_m \end{aligned}$$

$$\begin{aligned} \varphi_B &= \varphi_m \sin(180 - 240) \\ &= -0.866 \varphi_m \end{aligned}$$

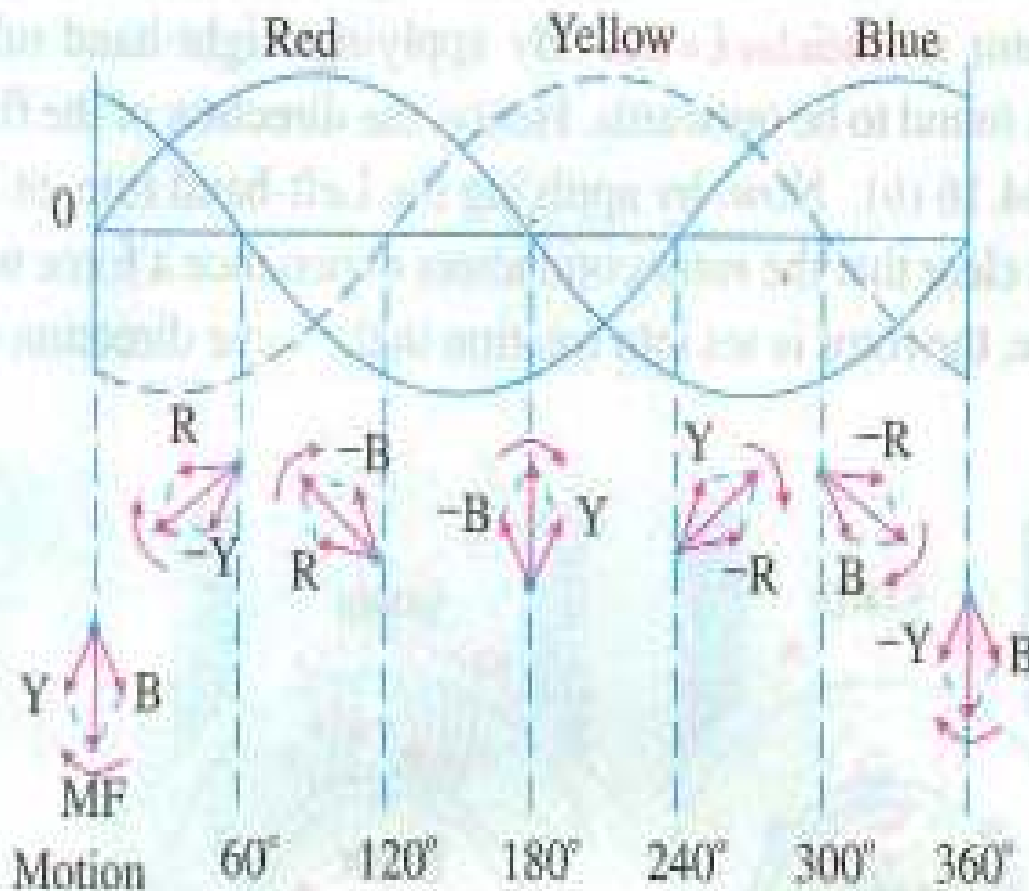
$$\varphi_T = 1.5 \varphi_m$$



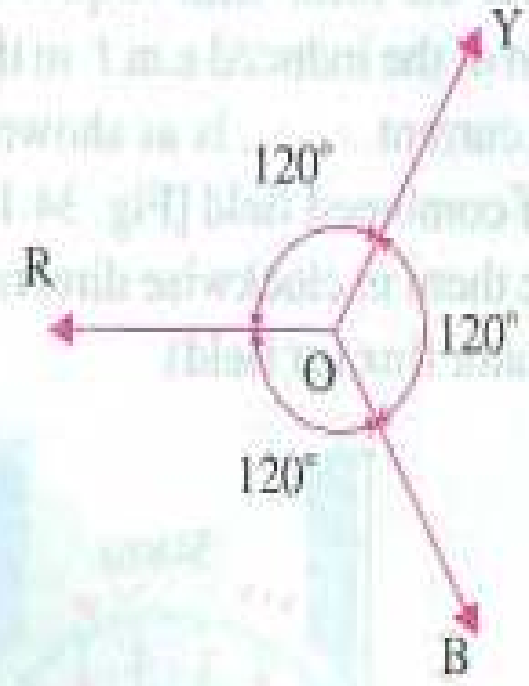


*Rotating Magnetic Field*  
*Magnetic Field*





(a)



(b)

## Speed and Slip

- IM can't run at synchronous Speed.
- Let consider for a moment that is rotor is rotating at synchronous speed.
- Under this condition there would be no cutting of flux by the rotor conductor and there would be no generated voltage no current and no torque.
- So, rotor speed is slightly less than synchronous speed.
- The difference between the synchronous speed and actual speed is called slip speed.

$N_s$  = Synchronous Speed in r.p.m.

$N_r$  = Actual Rotor speed in r.p.m.

Slip Speed =  $(N_s - N_r)$  r.p.m.

➤ Per-unit slip is usually called the Slip,

$$\text{Slip (S)} = \frac{N_s - N_r}{N_s} \text{ per unit (p.u)}$$

$$\text{Percentage Slip} = \frac{N_s - N_r}{N_s} \times 100$$

## Frequency of Rotor Voltage and Current

➤ Frequency of current and voltage in the stator must be same as the supply frequency.

$$f = \frac{P \times N_s}{120}$$

$$N_s = \frac{120 \times f}{P}$$

➤ Rotor frequency is given by,

$$f_r = \frac{P \times (N_s - N_r)}{120}$$

Now, 
$$\frac{f_r}{f} = \frac{N_s - N_r}{N_s}$$

$$\frac{f_r}{f} = S$$

$$f_r = S \times f$$

Case:1 Rotor is Stationary  
( $N_r=0$ )

$$S = \frac{N_s - N_r}{N_s} = 1$$

$$f_r = f$$

Case:2 Rotor is rotate at synch. Speed  
( $N_r=N_s$ )

$$S = \frac{N_s - N_r}{N_s} = 0$$

$$f_r = 0$$

## Rotor Current

### ➤ Stand Still Condition:

$E_{20}$  = e.m.f. induced per phase of the rotor at stand still

$R_2$  = Rotor resistance per phase

$X_{20}$  = Reactance per phase of the rotor at stand still =  $2\pi f_1 L_2$

$Z_{20}$  = Rotor Impedance per phase at stand still

$I_{20}$  = Rotor Current per phase at stand still

$$Z_{20} = R_2 + jX_{20}$$

$$I_{20} = \frac{E_{20}}{Z_{20}}$$

Power Factor at Stand Still

$$\cos \phi_{20} = \frac{R_2}{Z_{20}} = \frac{R_{20}}{\sqrt{R_2^2 + X_{20}^2}}$$

## ➤ Rotor Current at Slip(S):

- Induced e.m.f. per phase in the rotor winding at slip(s) is,

$$E_{2s} = SE_{20}$$

- Rotor winding resistance per phase =  $R_2$
- Rotor winding reactance per phase at Slip(S),

$$X_{2s} = 2\pi f_2 L = 2\pi (Sf_1) L = SX_{20}$$

- Rotor winding reactance per phase at slip(S)

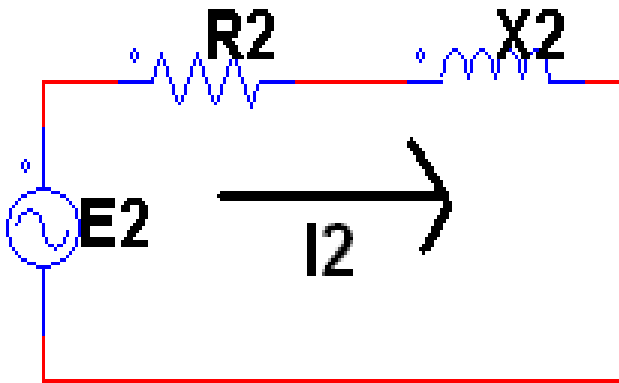
$$Z_{2s} = R_2 + jX_{2s} = R_2 + jSX_{20}$$

- Rotor Current at Slip(S) is

$$I_{2s} = \frac{E_{2s}}{Z_{2s}}$$

- Power Factor at Slip(S) is

$$\cos \phi_{2s} = \frac{R_2}{Z_{2s}}$$



$$I_2 = \frac{E_2}{Z_2} = \frac{E_2}{\sqrt{R_2^2 + X_2^2}}$$

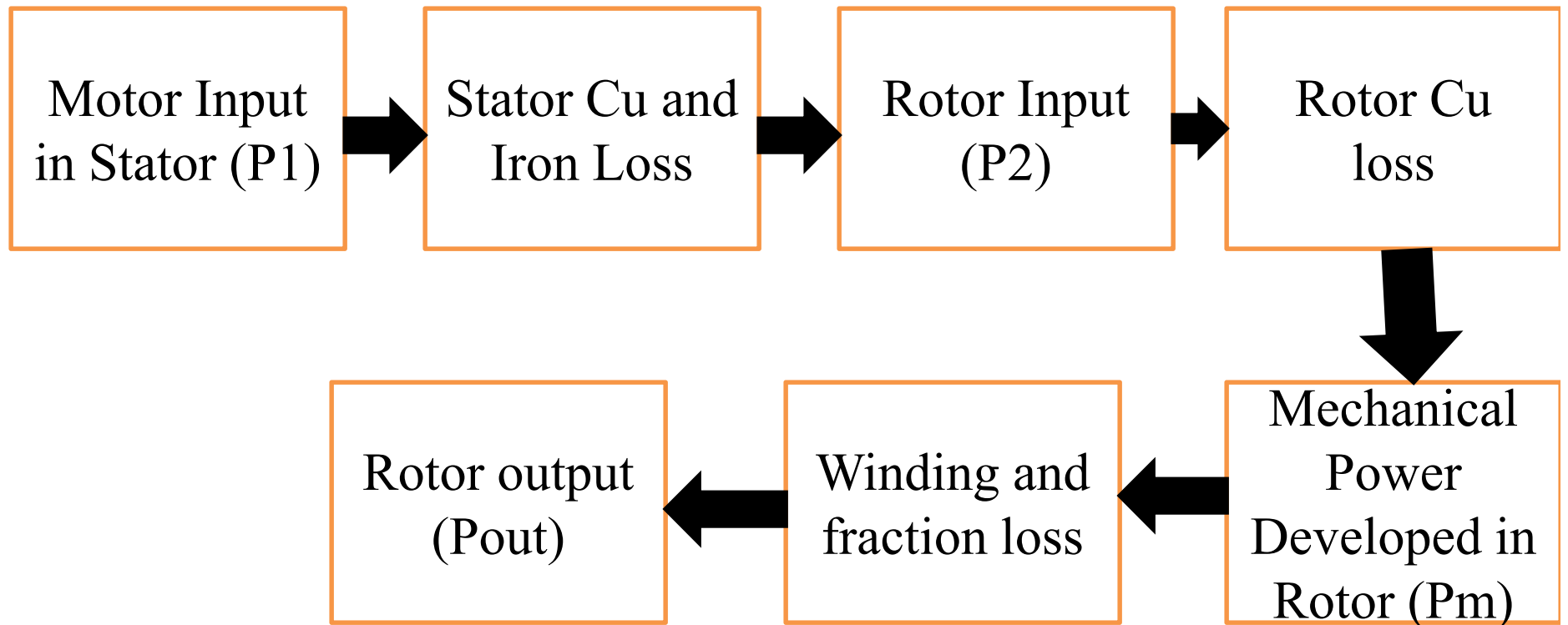
$$I_{2r} = \frac{E_{2r}}{Z_{2r}} = \frac{SE_2}{\sqrt{R_2^2 + (SX_2)^2}}$$

$$\cos \phi_2 = \frac{R_2}{Z_2} = \frac{R_2}{\sqrt{R_2^2 + X_2^2}}$$

$$\cos \phi_2 = \frac{R_2}{Z_{2r}} = \frac{R_2}{\sqrt{R_2^2 + (SX_2)^2}}$$



## POWER STAGE DIAGRAM OF AN IM



$$\text{Total Rotor Cu-loss} = 3I_2^2R_2$$

## TORQUE EQUATION

➤ Torque developed in IM on following factor:

1. The Part of rotating magnetic field which reacts with rotor and is responsible to produce induced e.m.f. in rotor.
2. The magnitude of rotor current in running condition
3. The power factor of rotor circuit in running condition

$$T \propto \phi \times I_{2r} \times \cos \phi_{2r}$$

$\phi$  = flux responsible to produce induced e.m.f

$I_{2r}$  = Rotor running Current

$\cos \phi_{2r}$  = Running power factor of rotor

➤ The flux( $\phi$ ) produced by stator is proportional to  $E_1$  i.e. Stator Voltage

$$\phi \propto E_1$$

➤ Ratio of stator turns to rotor turns i.e.  $k$

$$\frac{E_2}{E_1} = k$$

$$E_2 \propto \phi$$

While,

$$I_{2r} = \frac{E_{2r}}{Z_{2r}} = \frac{SE_{2r}}{\sqrt{R_2^2 + (SX_2)^2}}$$

$$\cos \phi_{2r} = \frac{R_2}{Z_{2r}} = \frac{R_2}{\sqrt{R_2^2 + (SX_2)^2}}$$

Now put all value of  $I_{2r}$ ,  $\cos \phi_{2r}$  and  $\phi$  in Torque equation,

$$T \propto E_2 \frac{SE_2}{\sqrt{R_2^2 + (SX_2)^2}} \frac{R_2}{\sqrt{R_2^2 + (SX_2)^2}}$$

$$T \propto \frac{SE_2^2 R_2}{R_2^2 + (SX_2)^2} N - m$$

$$T = \frac{kSE_2^2 R_2}{R_2^2 + (SX_2)^2} N - m$$

For 3-phase IM

$$k = \frac{3}{2\pi N_s}$$

$N_s$  = Synchronous Speed in r.p.s. =  $N_s/60$

$$T = \frac{3}{2\pi N_s} \frac{SE_2^2 R_2}{R_2^2 + (SX_2)^2} N - m$$

➤ Starting Torque:

At  $N=0$  ;  $S=1$

$$T_{st} = \frac{3}{2\pi N_s} \frac{E_2^2 R_2}{(R_2^2 + X_2^2)} N - m$$

➤ Changing  $R_2$ , starting Torque can be controlled.

➤ Changing  $R_2$  at start is possible in case of slip ring IM only.

## Condition For Maximum Torque

- Torque depend on slip at which motor is running
- Supply voltage to the motor is usually rated and constant also fixed ratio between E1 and E2.
- So, E2 is constant
- Similarly R2 , X2 and Ns are Constant for IM.
- For Maximum Torque → Torque is only control by Slip(S).

$$\frac{dT}{dS} = 0$$

Now,

$$T = \frac{kSE_2^2 R_2}{R_2^2 + (SX_2)^2}$$

Here R2 , X2 and K are Constant

Now,

$$\frac{dT}{dS} = 0$$

$$S^2 X_2^2 - R_2^2 = 0$$

$$S^2 = \frac{R_2^2}{X_2^2}$$

$$S = \frac{R_2}{X_2} \text{ Neglecting (-ve) slip}$$

➤ This is the slip at which torque is maximum and is denoted as ( $S_m$ )

$$S_m = \frac{R_2}{X_2}$$

## Magnitude of Max. Torque

$$S_m = \frac{R_2}{X_2}$$

➤ Now put value in torque equation.

$$\begin{aligned} T_m &= \frac{k S_m E^2 R_2}{R_2^2 + (S_m X_2)^2} \\ &= \frac{k \left( \frac{R_2}{X_2} \right) E^2 R_2}{R_2^2 + \left( \frac{R_2}{X_2} X_2 \right)^2} \end{aligned}$$

$$T_m = \frac{k E^2}{2 X_2} \text{ N - m}$$



- Max. Torque is inversely proportional to the rotor reactance.
- It is directly proportional to the square of the rotor induced e.m.f. at stand still.
- It is not depend on the rotor resistance  $R_2$ .

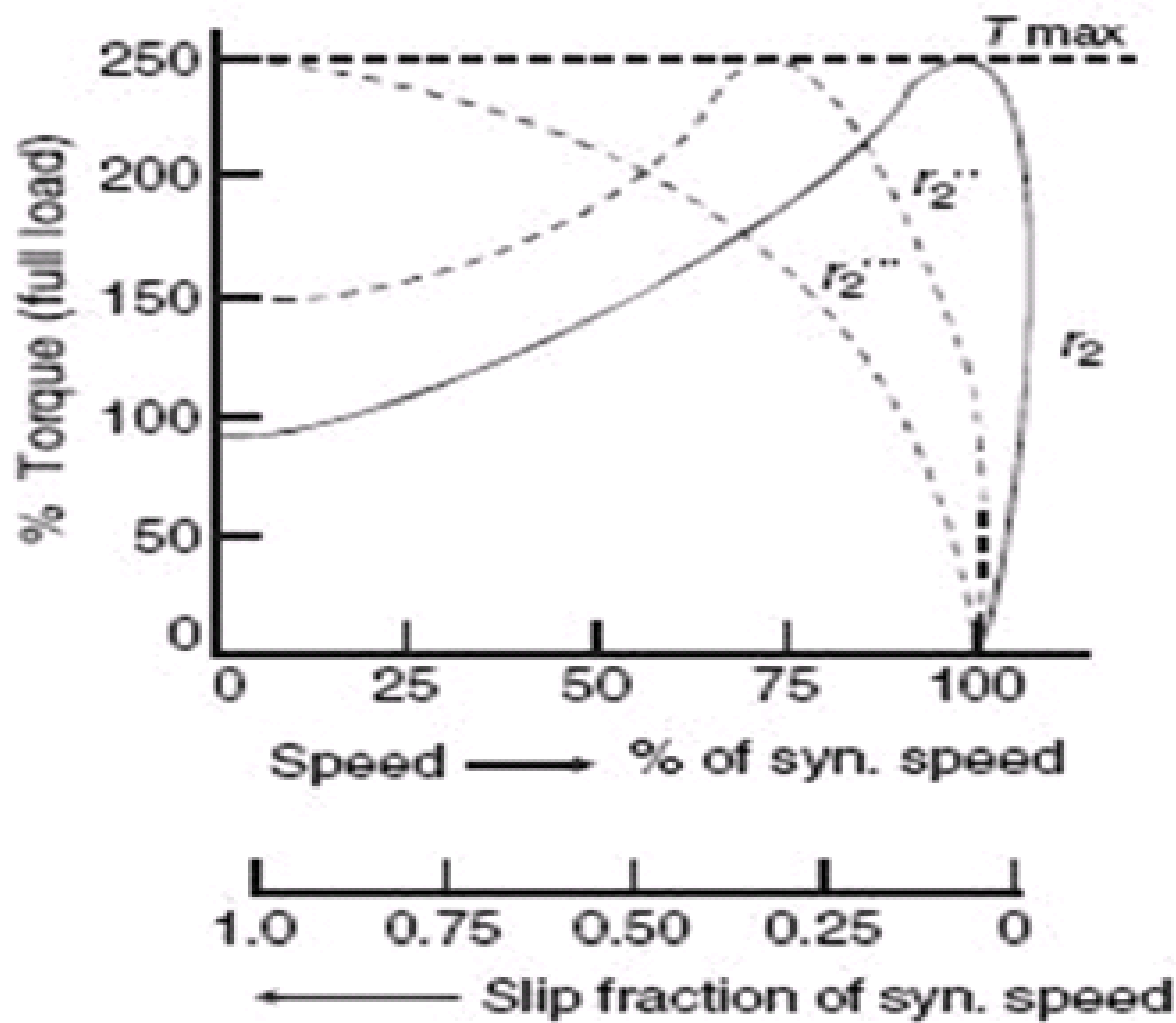
## Torque-Slip and Torque-Speed characteristics.

We know that,

$$T = \frac{kSE^2 R_2}{R_2^2 + (SX_2)^2}$$

➤  $R_2$  and  $X_2$  are Constant. So, Torque depend upon Slip(S)

1. Low-Slip Region
2. Medium-Slip Region
3. High-Slip Region



# Losses in Induction Motor

## 1. Constant Losses

- Core Losses
- Mechanical Losses

## 2. Variable Losses

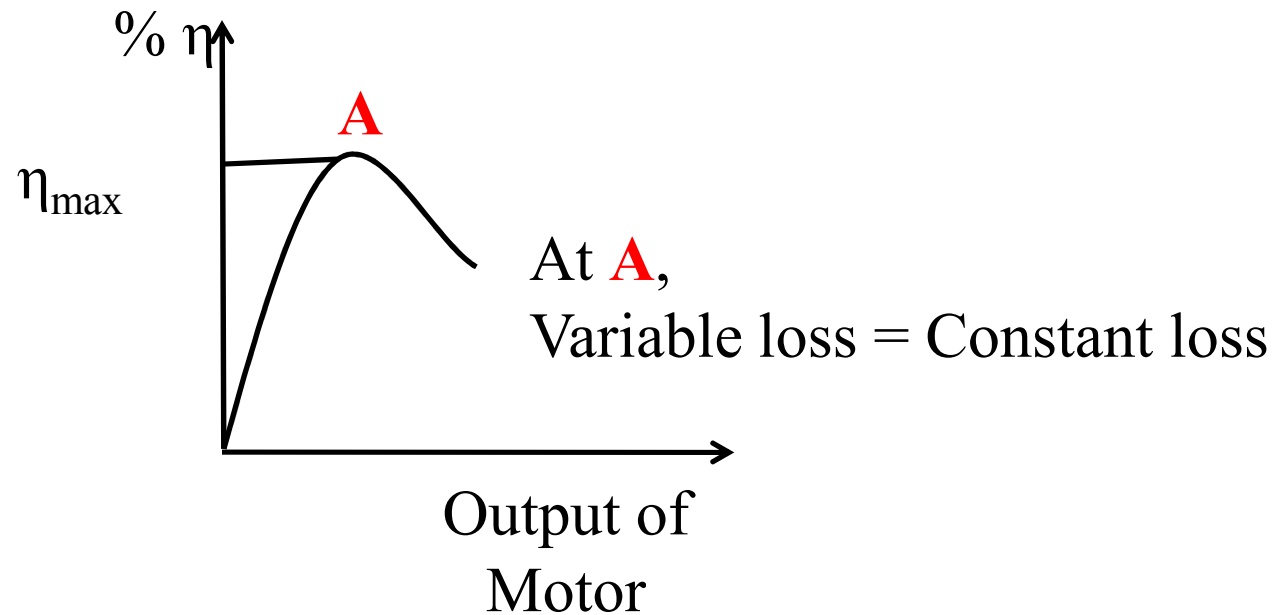
- Copper Losses in Stator
- Copper Losses in Rotor

$$\text{Total Rotor Cu-loss} = 3I_2^2R_2$$

## Efficiency of an Induction Motor

➤ The Ratio of net power available at the shaft ( $P_{out}$ ) and the net electrical power input ( $P_{in}$ ) to the motor is called as overall efficiency of an induction motor

$$\% \eta = \frac{P_{out}}{P_{in}} \times 100$$



## ● *Working principle:-*

- **The single-phase induction motor operation can be described by two methods:**

**1) Double revolving field theory    2) Cross-field theory.**

- **Double revolving theory is perhaps the easier of the two explanations to understand**

- **Double revolving field theory:-**
- **A single-phase ac current supplies the main winding that produces a pulsating magnetic field.**
- **Mathematically, the pulsating field could be divided into two fields, which are rotating in opposite directions.**
- **The interaction between the fields and the current induced in the rotor bars generates opposing torque .**

- **Double revolving field theory:-**
- **The interaction between the fields and the current induced in the rotor bars generates opposing torque.**
- **Under these conditions, with only the main field energized the motor will not start.**
- **However, if an external torque moves the motor in any direction, the motor will begin to rotate.**



## ● **Double revolving field theory:-**

- **The pulsating field is divided a forward and reverse rotating field**
- **Motor is started in the direction of forward rotating field this generates small (5%) positive slip**

$$S_r = N_s - N_r / N_s$$

- **Reverse rotating field generates a larger (1.95%) negative slip**

$$S_b = N_s + N_r / N_s$$

## ● **Construction of single phase induction motor:-**

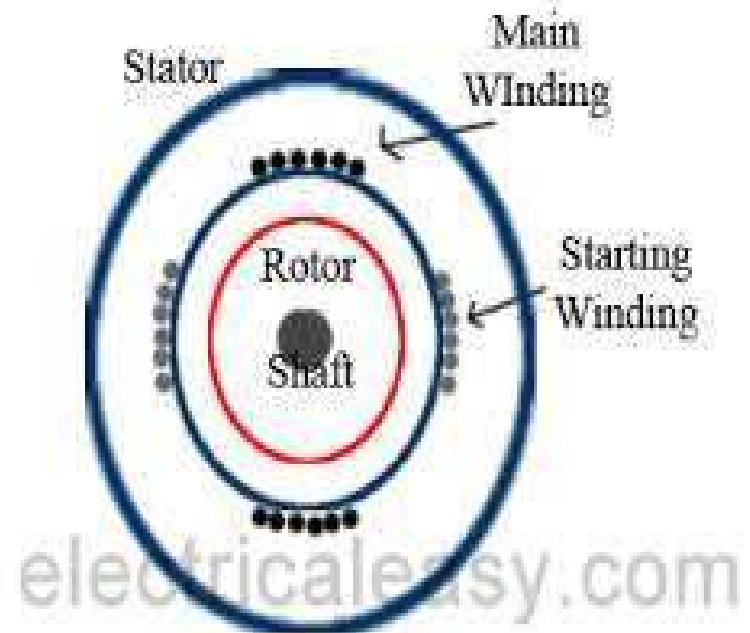
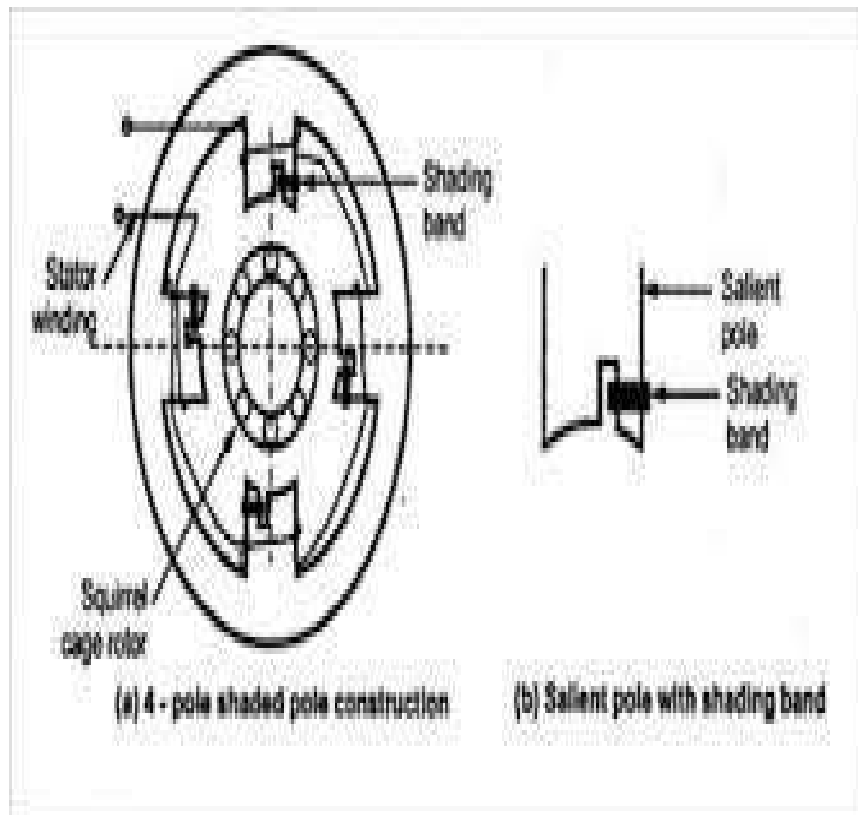
Construction of a **single phase IM** is similar to 3-

phase **squirrel cage induction motor**. The **rotor** used here is same as that used in 3 phase squirrel cage Induction motor and it is very simple in design, robust in construction. The rotor is not insulated from the core. The slots on rotor are either semi-closed type or totally closed type. Rotor windings are perfectly symmetrical

## ● **Construction of single phase induction motor:-**

Single phase motor can be wound for any even number of poles i.e two, four, six, etc. This type of motor normally have two **Stator** windings. In motors that operate with both windings energized ,the winding with more wire (more turns) is known as main winding and the other is called auxiliary winding. In case of this motor synchronous speed equation is  $(N$

# ● Construction of single phase induction motor:-



- **Types of single phase induction motor:-**

**According to the method used for it's starting single phase**

**I.M. can be classified into following types:-**

- 1)Split phase motor/ Resistance start motor**
- 2)Capacitor start motor**
- 3)Capacitor start-Capacitor run motor**
- 4)Two value capacitor motor**
- 5)Shaded pole motor**

- **Split phase motor:-**

**A split phase induction motor consist of two main parts:-**

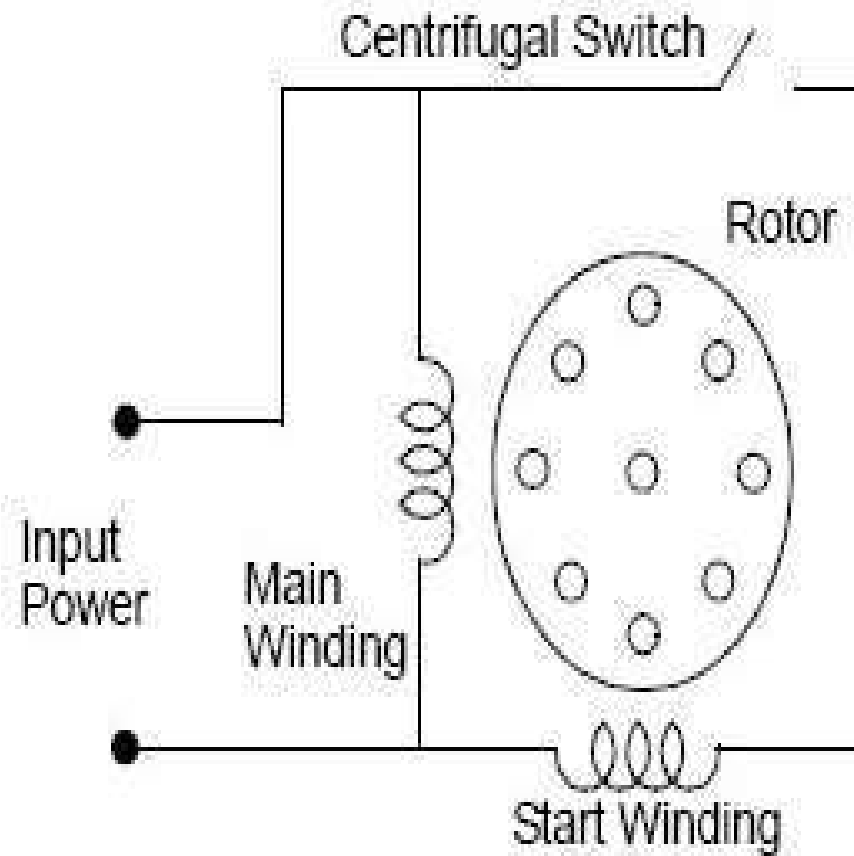
**1) Stator 2) Rotor**

**The stator is provided with single phase windings**

**a)Main winding      b)Auxiliary winding**

**The two winding are placed 90 degree electrical apart & are connected in parallel across the single phase AC supply. Whereas the auxiliary winding has a high resistance & low reactance.**

- **Split phase motor:-**



- **Capacitor Start Motor:-**

- **In these motors, a capacitor is connected in series with the starting winding , which takes leading current & hence produce high starting torque.**

- **The capacitor motor can be classified as :-**

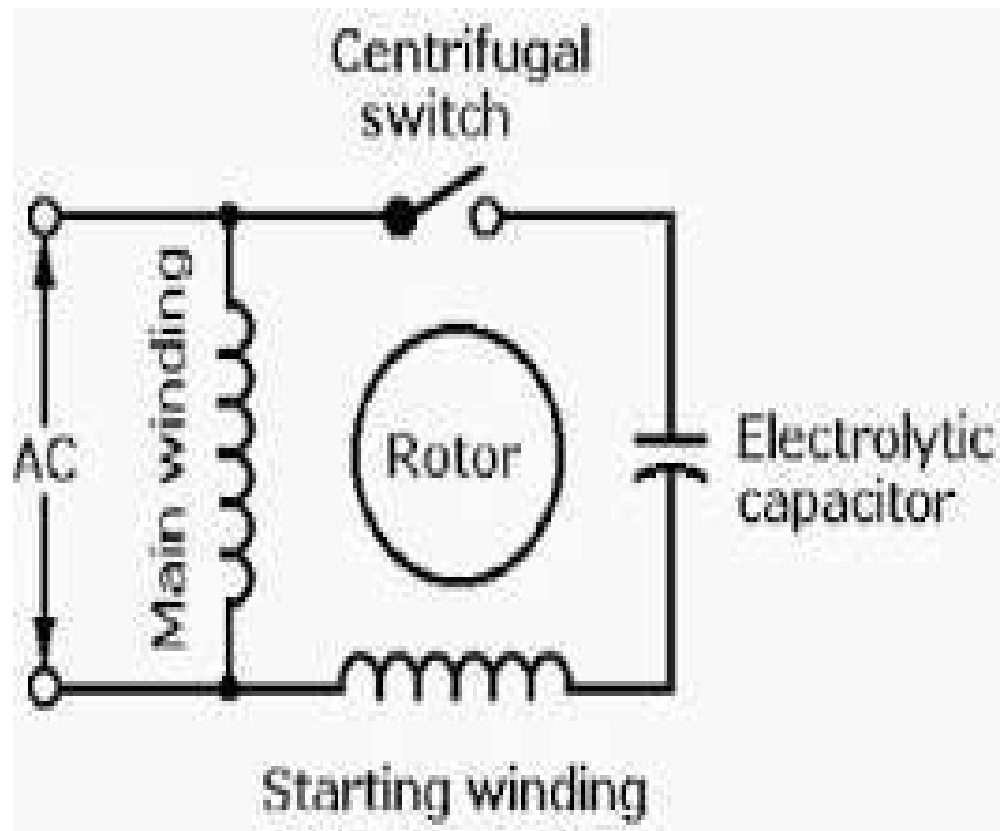
- 1.capacitor start**

- 2.capacitor start & capacitor run**

- 3.Two value capacitor motor**

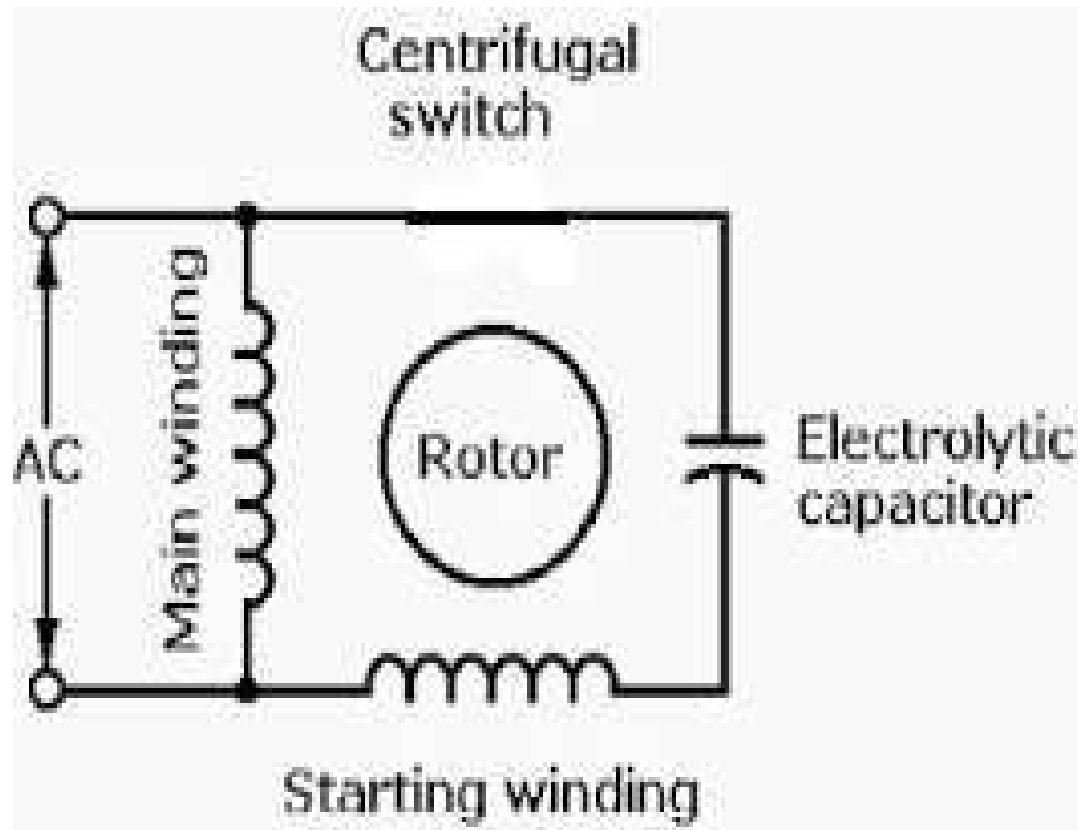


- **Capacitor start motor:-**
- **In this motor the capacitor is connected in series with the starting winding which takes leading current.**
- **As the capacitor is used only at start , it is rated for intermittent duty & the cost of which decreases.**
- **A relatively small ac electrolytic type capacitor is used.**
- **This motor has high starting torque, about 1.5 times the full-load torque.**



## ● **Capacitor start & Capacitor run motor:-**

- **In this motor there is no centrifugal switch, so the capacitor remains in the circuit & helps to improve the power factor under running condition.**
- **The power factor of this motor under running condition is high.**
- **The operation is also quiet & smooth.**
- **The torque under running condition is also higher than the capacitor start &**



- **Two value capacitor type motor:-**

**This types of motor employs two capacitor 1)Start capacitor( $C_s$ )**

**2)Run Capacitor( $C_r$ )**

**The Start capacitor is rated for short rating & is used for starting.**

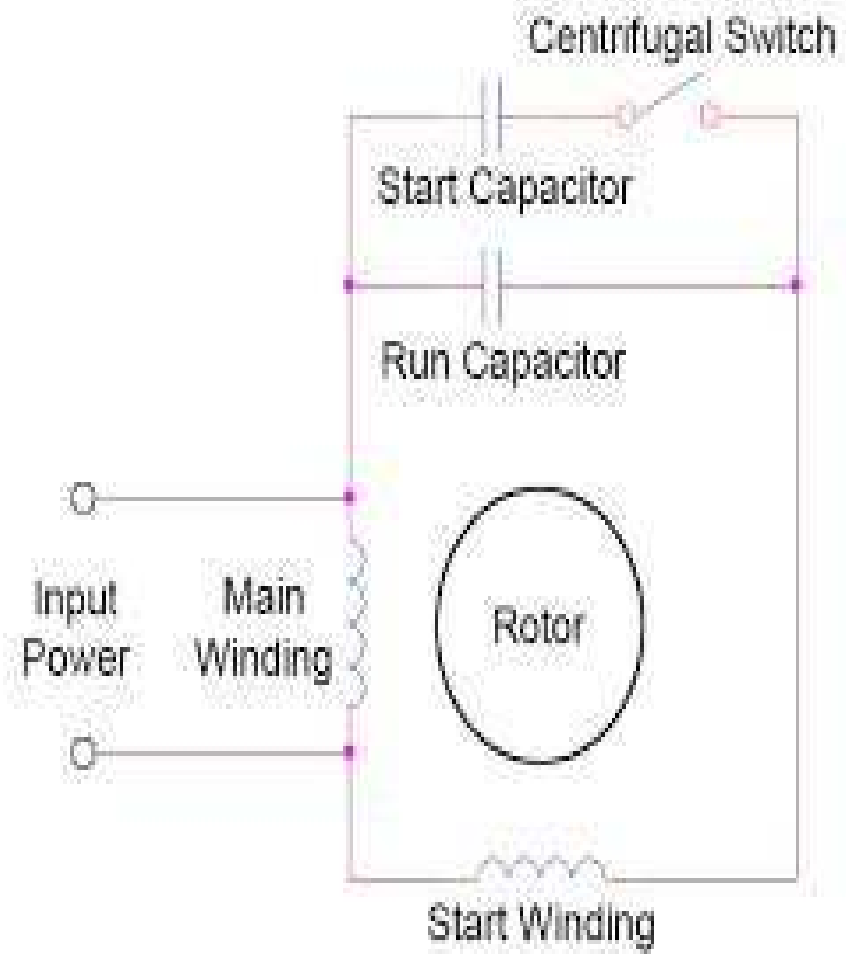
**The Run capacitor is rated for continuous duty as it is used under**

- **Two value capacitor type motor:-**

**A centrifugal switch is used to disconnect the start capacitor when the motor has reached about 70 to 80% of its full load speed.**

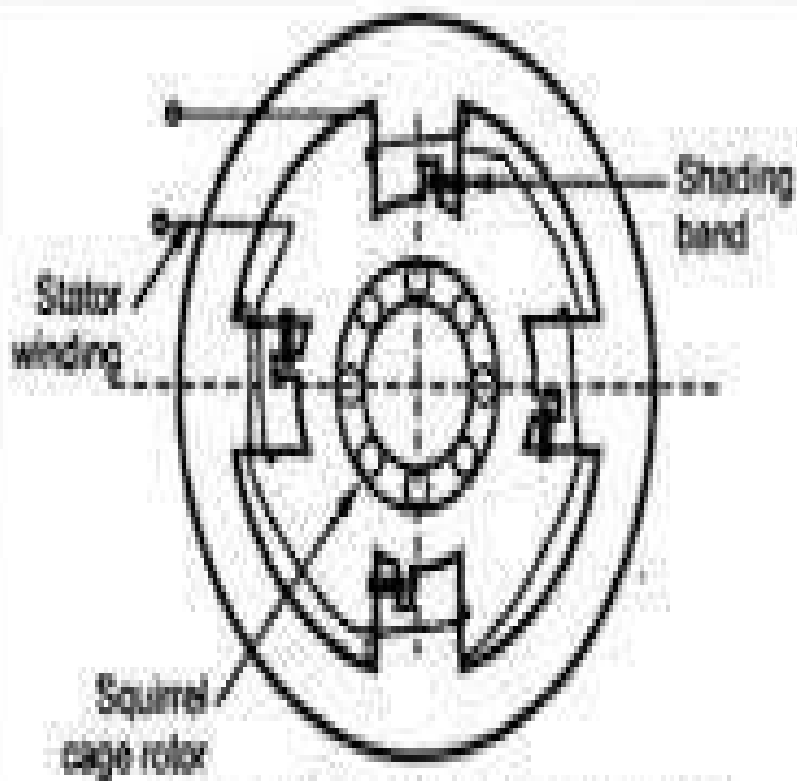
**This motor is useful where the motor has start against heavy loads.**

**The starting torque is about 2 to 2.5 times its full load torque.**

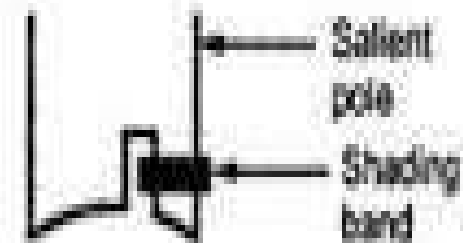


- **Shaded pole motor:-**
- **A shaded pole motor has a stator consisting of salient poles & a squirrel cage rotor.**
- **The main winding is wound on the entire pole section.**
- **When the ac supply is given to the stator winding of shaded pole motor , due to shading provided on the salient poles, a rotating magnetic field is produced.**





(a) 4 - pole shaded pole construction



(b) Salient pole with shading band

Thank you

